

# MSSM and $B$ physics

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Fourth Mass Origin Workshop, Tsukuba, 8Mar2006

Based on

- P. Ko, G. Kramer, [J.-h. Park](#), EPJC25(2002)
- G. L. Kane, P. Ko, C. Kolda, [J.-h. Park](#), Haibin Wang, Lian-Tao Wang, PRL90(2003), PRD70(2004)
- P. Ko, A. Masiero, [J.-h. Park](#), PRD72(2005).

# CKM matrix

- Mixing matrix connecting weak interaction eigenstates and mass eigenstates of quarks.

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- CKM matrix is **hierarchical** and has one **CP** phase.

$$V = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

- Unitarity condition,  $V^\dagger V = VV^\dagger = \mathbf{1}$ , yields unitarity triangles.

# Unitarity triangle on the $(\rho, \eta)$ plane

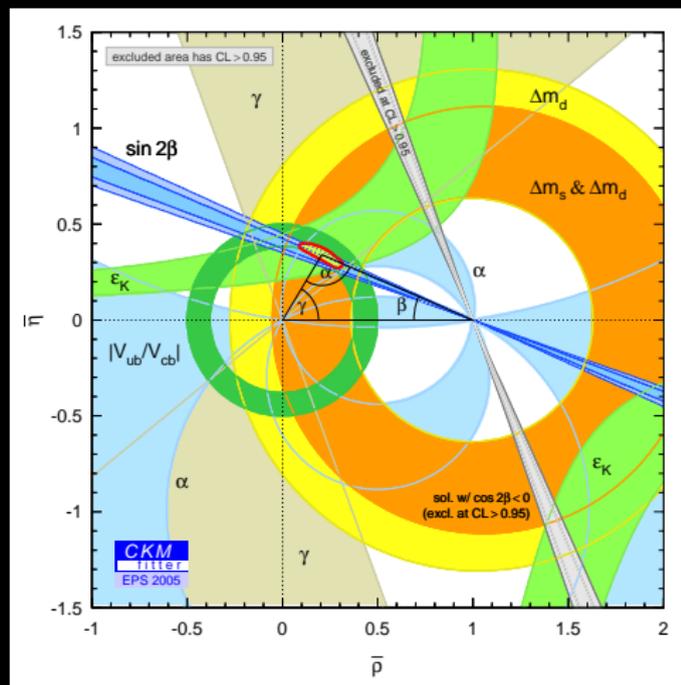
- SM fit of  $(\rho, \eta)$
- In the presence of new physics, constraints on  $(\rho, \eta)$  coming from loop level processes such as  $\varepsilon_K, \Delta m_d$ , and  $\Delta m_s$ , may be weaker.

→

$\gamma$ -as-a-free-variable strategy.

- $\gamma$  is not longer free even with loop level new physics due to constraints from  $B \rightarrow DK$ .

$$\gamma(DK) = (63_{-13}^{+15})^\circ.$$



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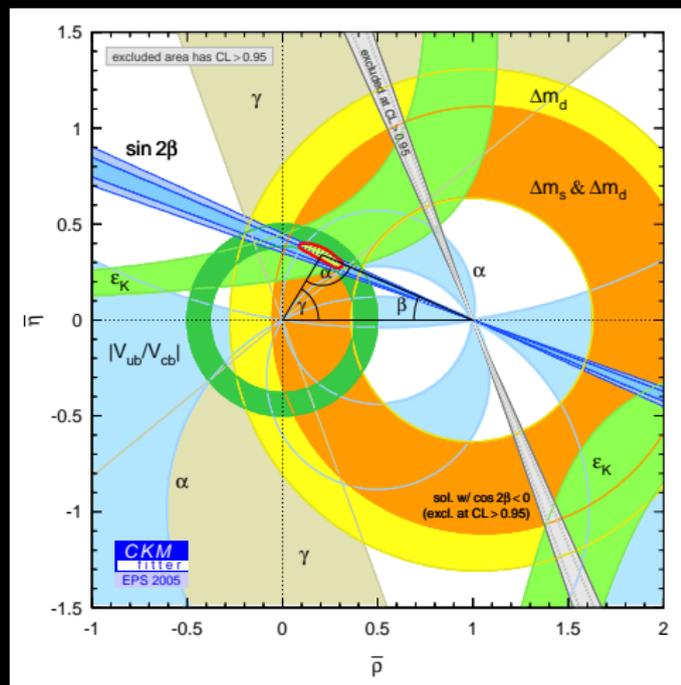
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# SUSY FCNC/CP problem

- Many of soft SUSY breaking parameters are complex and flavor violating, and a generic supersymmetric standard model results in huge flavor and CP violation.
- There should be a mechanism which controls FCNC and CP. This may be due to the SUSY breaking/mediation mechanism and/or flavor symmetry. We can get a clue to these mechanisms by studying FCNC and CP violation in supersymmetric models.
- Mass insertion approximation is a useful tool to present flavor violation through sfermions.

$(\delta_{12}^d)_{LL}$  : dimensionless transition strength from  $\tilde{s}_L$  to  $\tilde{d}_L$ .

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# Weak effective Hamiltonian

$$H_{\text{eff}}^{\Delta B=1} = \sum_{p=u,c} [C_1^p O_1^p + C_2^p O_2^p] + \sum_{i=3}^6 C_i O_i + C_{7\gamma} O_{7\gamma} + C_{8g} O_{8g} + \text{h.c.}$$

- Current-current operators

$$O_1^p = (\bar{p}b)_{V-A} (\bar{s}p)_{V-A}$$

$$O_2^p = (\bar{p}_\alpha b_\beta)_{V-A} (\bar{s}_\beta p_\alpha)_{V-A}$$

- QCD penguin operators

$$O_3 = (\bar{s}b)_{V-A} \sum_q (\bar{q}q)_{V-A}$$

$$O_4 = (\bar{s}_\alpha b_\beta)_{V-A} \sum_q (\bar{q}_\beta q_\alpha)_{V-A}$$

$$O_5 = (\bar{s}b)_{V-A} \sum_q (\bar{q}q)_{V+A}$$

$$O_6 = (\bar{s}_\alpha b_\beta)_{V-A} \sum_q (\bar{q}_\beta q_\alpha)_{V+A}$$

- (Chromo)magnetic penguin operators

$$O_{7\gamma} = -\frac{e}{8\pi^2} m_b \bar{s} \sigma_{\mu\nu} (1 + \gamma_5) F^{\mu\nu} b$$

$$O_{8g} = -\frac{g_s}{8\pi^2} m_b \bar{s} \sigma_{\mu\nu} (1 + \gamma_5) G^{\mu\nu} b$$

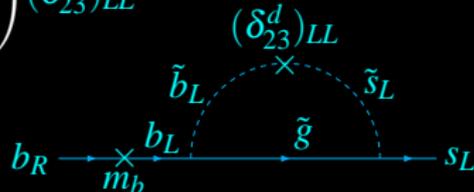
# Gluino-squark loop contributions to Wilson coefficients

Gabbiani, Gabrielli, Masiero, Silvestrini, NPB(1996)  
 With S. Baek, J. H. Jang, P. Ko, NPB(2001)

- QCD penguin operators

Beware typos.

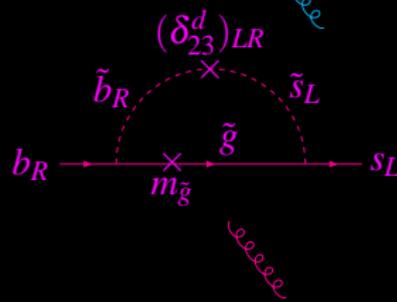
$$C_{3,\dots,6} = -\frac{\alpha_s^2}{4\tilde{m}^2} \left( \text{Diagram 1} + \text{Diagram 2} \right) (\delta_{23}^d)_{LL}$$



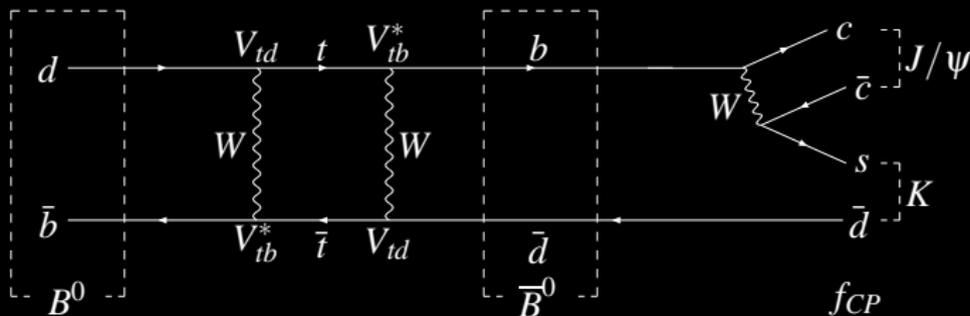
- Magnetic operators

$$C_{7\gamma} = -\frac{4\pi Q_b \alpha_s}{3\tilde{m}^2} \left[ (\delta_{23}^d)_{LL} M_4(x) - (\delta_{23}^d)_{LR} \left( \frac{m_{\tilde{g}}}{m_b} \right) 4B_1(x) \right],$$

$$C_{8g} = -\frac{\pi \alpha_s}{\tilde{m}^2} \left[ (\delta_{23}^d)_{LL} \left( \frac{3}{2} M_3(x) - \frac{1}{6} M_4(x) \right) + (\delta_{23}^d)_{LR} \left( \frac{m_{\tilde{g}}}{m_b} \right) \frac{1}{6} \left( 4B_1(x) - 9x^{-1} B_2(x) \right) \right]$$



# Overview of $CP$ violation in $B$ system



- Time dependent  $CP$  asymmetry

$$\mathcal{A}_{CP}(t) \equiv \frac{\Gamma(\overline{B^0}(t) \rightarrow f_{CP}) - \Gamma(B^0(t) \rightarrow f_{CP})}{\Gamma(\overline{B^0}(t) \rightarrow f_{CP}) + \Gamma(B^0(t) \rightarrow f_{CP})} = -C_{f_{CP}} \cos(\Delta m_d t) + S_{f_{CP}} \sin(\Delta m_d t),$$

$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}, \quad S_{f_{CP}} = \frac{2 \operatorname{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}, \quad \lambda_{f_{CP}} \equiv \mp e^{-2i(\beta + \theta_d)} \frac{\overline{A}(\overline{B^0} \rightarrow f_{CP})}{A(B^0 \rightarrow f_{CP})}$$

- $B^0$ - $\bar{B}^0$  mixing  $2m_B M_{12} \equiv \langle \overline{B^0} | H_{\text{eff}}^{\Delta B=2} | B^0 \rangle = \frac{1}{2} \Delta m_d e^{-i2(\beta + \theta_d)}$

# Outline

- 1  $B^0-\overline{B}^0$  mixing,  $B \rightarrow J/\psi K_S$ ,  $B \rightarrow X_d \gamma$  in general MSSM
- 2  $B_d \rightarrow \phi K_S$   $CP$  asymmetries as a probe of SUSY
- 3  $B_d \rightarrow \phi K_S$   $CP$  asymmetry and  $\varepsilon'/\varepsilon_K$
- 4 Summary

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Possible SUSY effects on  $b \rightarrow d$  transitions

With P. Ko, G. Kramer, EPJC(2002)

- Mass insertion approximation with  $m_{\tilde{g}} = \tilde{m} = 500$  GeV
- Scan over one of  $\delta_{13}^d$ 's as well as  $\gamma$ .
- Constraints

$$\Delta m_d = (0.472 \pm 0.017) \text{ ps}^{-1}, \quad \sin 2\beta_{J/\psi} = 0.79 \pm 0.10,$$

$$\underline{B(B \rightarrow X_d \gamma) < 1 \times 10^{-5}}$$

- Predictions

$$A_{ll} \equiv \frac{N(BB) - N(\bar{B}\bar{B})}{N(BB) + N(\bar{B}\bar{B})} \approx \text{Im} \left( \frac{\Gamma_{12} \approx \Gamma_{12}^{\text{SM}}}{M_{12}^{\text{SM}} + M_{12}^{\text{SUSY}}} \right)$$

$$A_{\text{CP}}^{b \rightarrow d \gamma} \equiv \frac{\Gamma(B \rightarrow X_d \gamma) - \Gamma(\bar{B} \rightarrow \bar{X}_d \gamma)}{\Gamma(B \rightarrow X_d \gamma) + \Gamma(\bar{B} \rightarrow \bar{X}_d \gamma)}$$

- Consider two cases: Single  $(\delta_{13}^d)_{LL}$  insertion, Single  $(\delta_{13}^d)_{LR}$  insertion.

# LL insertion

- Hatched region for

$$B(B \rightarrow X_d \gamma) > 1 \times 10^{-5}.$$

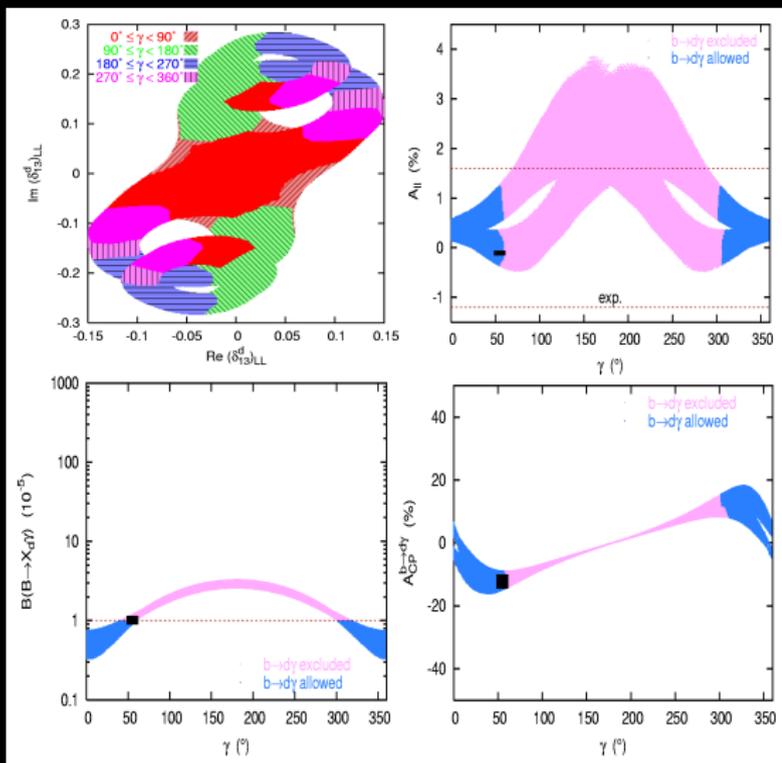
- $A_{ll}$  can have sign opposite to that of SM value.

- $B \rightarrow X_d \gamma$  strongly constrains  $|(\delta_{13}^d)_{LL}| \lesssim 0.2$

$$\rightsquigarrow -60^\circ \lesssim \gamma \lesssim 60^\circ.$$

- Imposing

$B(B \rightarrow X_d \gamma) > 1 \times 10^{-6}$   
does not make any  
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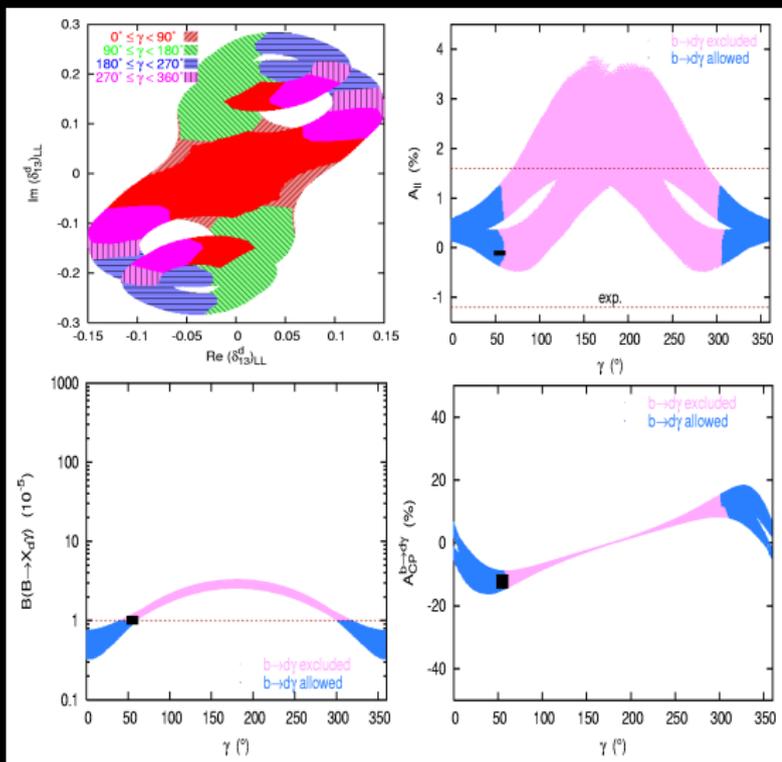
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# LR insertion

- Hatched region for

$$B(B \rightarrow X_d \gamma) > 1 \times 10^{-5}.$$

- Not much effect on  $A_{ll}$ .

- $B \rightarrow X_d \gamma$  even more strongly constrains

$$|(\delta_{13}^d)_{LR}| \lesssim 10^{-2}$$

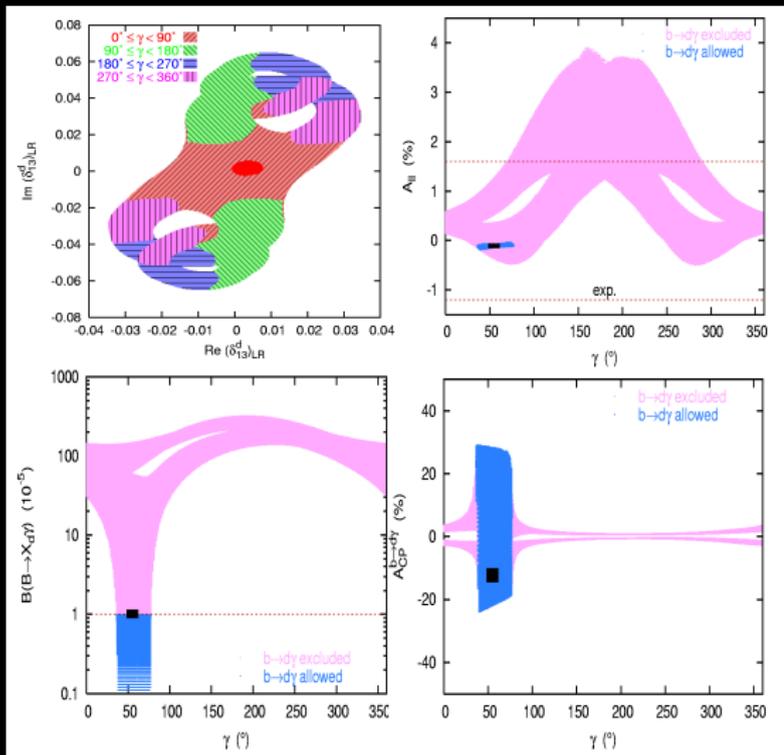
$$\rightsquigarrow 30^\circ \lesssim \gamma \lesssim 80^\circ.$$

- Nevertheless,

$$-25\% \lesssim A_{CP}^{b \rightarrow d \gamma} \lesssim +30\%.$$

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- $B \rightarrow X_d \gamma$  even more strongly constrains

$$|(\delta_{13}^d)_{LR}| \lesssim 10^{-2}$$

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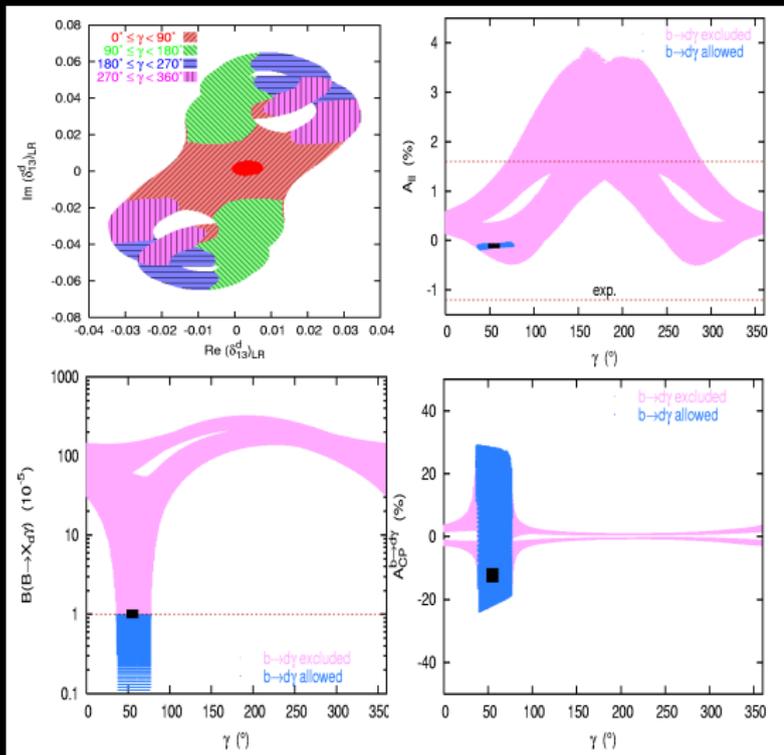
- Nevertheless,

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# Outline

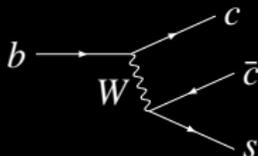
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# Why $B_d \rightarrow \phi K_S$ ?

- Absence of tree level diagram in the Standard Model  
 → Sensitive to New Physics.



- Compare  $B_d \rightarrow J/\psi K_S$ :



# CPV measurements did not agree with SM very well

- SM prediction

$$\lambda_{\phi K}^{\text{SM}} = -e^{-2i\beta},$$

$$C_{\phi K}^{\text{SM}} = \frac{1 - |\lambda_{\phi K}^{\text{SM}}|^2}{1 + |\lambda_{\phi K}^{\text{SM}}|^2} = 0,$$

$$S_{\phi K}^{\text{SM}} = \frac{2 \text{Im}\lambda_{\phi K}^{\text{SM}}}{1 + |\lambda_{\phi K}^{\text{SM}}|^2} = \sin 2\beta = 0.734 \pm 0.054$$

- Measurements

	$S_{\phi K}$	$C_{\phi K}$
BaBar <sup>1</sup>	$+0.45 \pm 0.43 \pm 0.07$	$-0.38 \pm 0.37 \pm 0.12$
Belle <sup>2</sup>	$-0.96 \pm 0.50^{+0.09}_{-0.11}$	$+0.15 \pm 0.29 \pm 0.07$
Average	$-0.15 \pm 0.33$	$-0.05 \pm 0.24$
Avg. - SM	$-2.7\sigma$	$-0.2\sigma$

<sup>1</sup>T. Browder, Talk at LP03.

<sup>2</sup>Belle Collaboration, PRL91(2003)

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- Measurements

	$S_{\phi K}$	$C_{\phi K}$
BaBar <sup>1</sup>	$+0.50 \pm 0.25^{+0.07}_{-0.04}$	$0.00 \pm 0.23 \pm 0.05$
Belle <sup>2</sup>	$+0.44 \pm 0.27 \pm 0.05$	$-0.14 \pm 0.17 \pm 0.07$
Average	$+0.47 \pm 0.19$	$-0.09 \pm 0.14$
Avg. – SM	$-1.1 \sigma$	$-0.6 \sigma$

<sup>1</sup>BABAR Collaboration, PRD(2005)

<sup>2</sup>Belle Collaboration, hep-ex/0507037



# Numerical analysis of gluino-squark loops

With G. L. Kane, P. Ko, C. Kolda, Haibin Wang, Lian-Tao Wang, PRL(2003), PRD(2004)

- Mass insertion approximation with  $m_{\tilde{g}} = \tilde{m} = 400$  GeV
- QCD factorization for hadronic matrix elements
- Scan over one of  $\delta_{23}^d$ 's such that

Beneke, Buchalla, Neubert, Sachrajda

$$2.0 \times 10^{-4} < B(B \rightarrow X_s \gamma) < 4.5 \times 10^{-4}, \quad \Delta M_s > 14.9 \text{ ps}^{-1}$$

A. Stocchi, hep-ph/0010222

# LL or RR for large $B_S - \bar{B}_S$ mixing

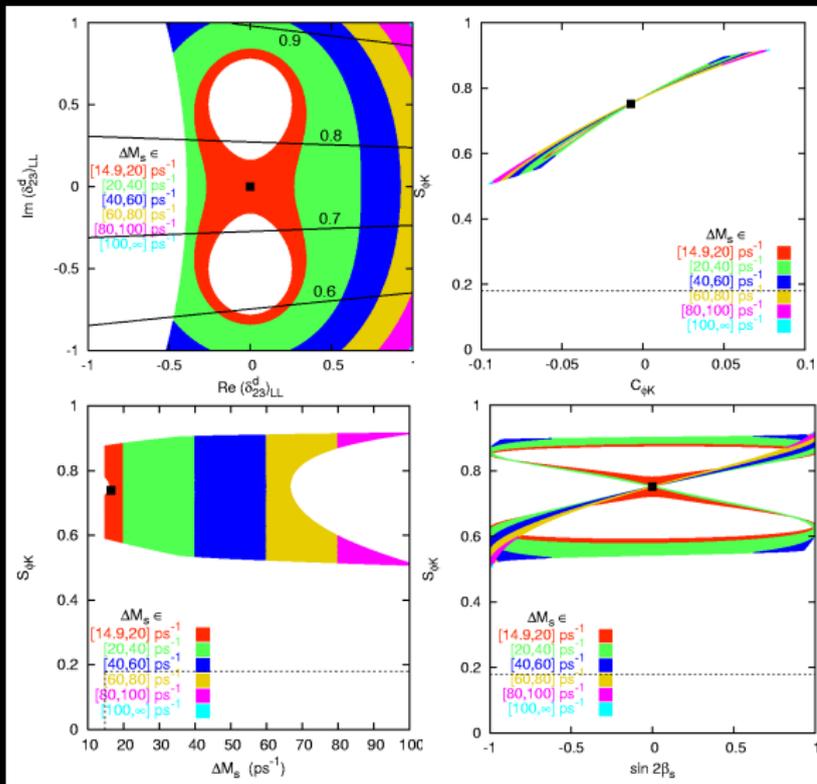
- LL plots for

$$m_{\tilde{g}} = \tilde{m} = 400 \text{ GeV.}$$

- $(\delta_{23}^d)_{LL}$  can not significantly lower  $S_{\phi K}$ .

$$S_{\phi K} \gtrsim 0.05 \quad \text{for} \\ m_{\tilde{g}} = \tilde{m} = 250 \text{ GeV.}$$

- But large effects possible in  $B_S - \bar{B}_S$  mixing
- RR is similar to LL except for  $B \rightarrow X_S \gamma$ .



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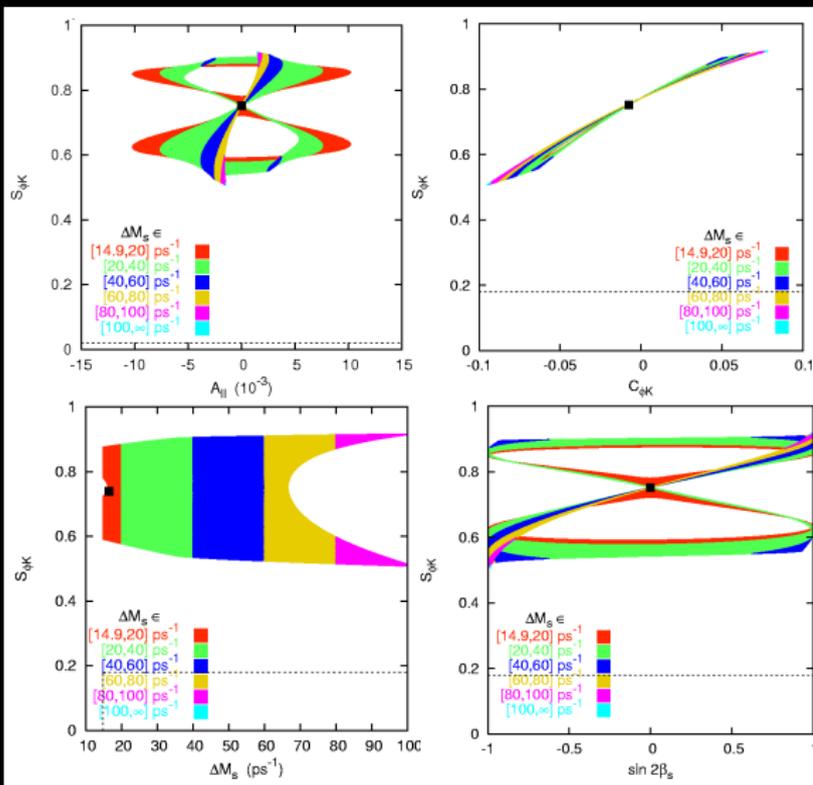
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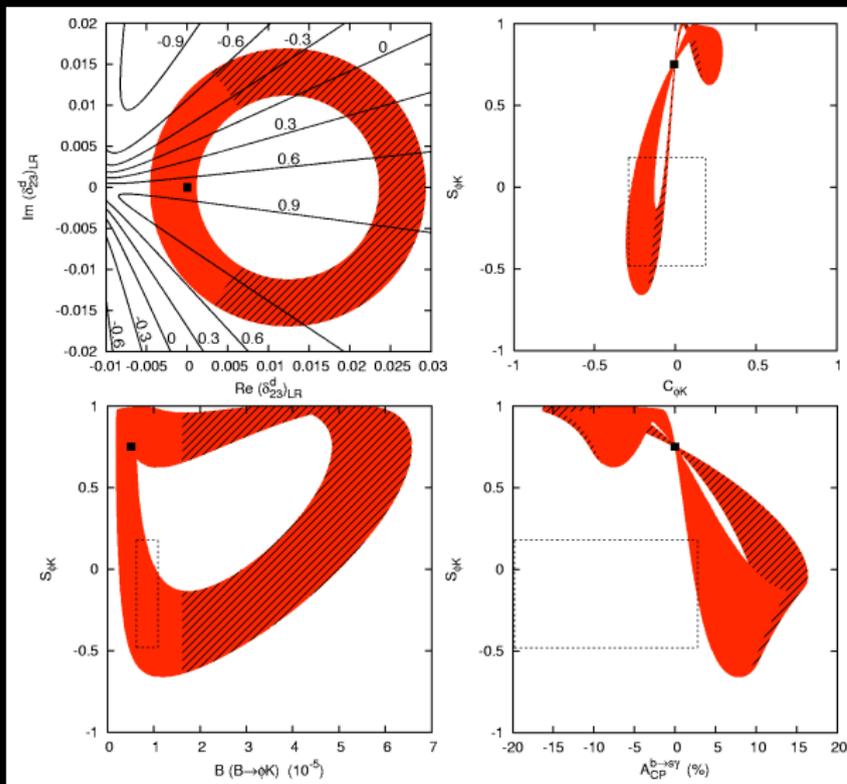


# LR or RL for big change of $S_{\phi K}$

- LR plots for

$$m_{\tilde{g}} = \tilde{m} = 400 \text{ GeV.}$$

- $-0.6 < S_{\phi K} < 1$   
for  $|(\delta_{23}^d)_{LR}| \sim 10^{-2}$ .
- Correlations between  $S_{\phi K}$  and  $C_{\phi K}$ ,  $S_{\phi K}$  and  $A_{\text{CP}}^{b \rightarrow s\gamma}$ .
- Hatched region for  $B(B \rightarrow \phi K) > 1.6 \times 10^{-5}$ .
- Not much effect on  $B_S - \bar{B}_S$  mixing.

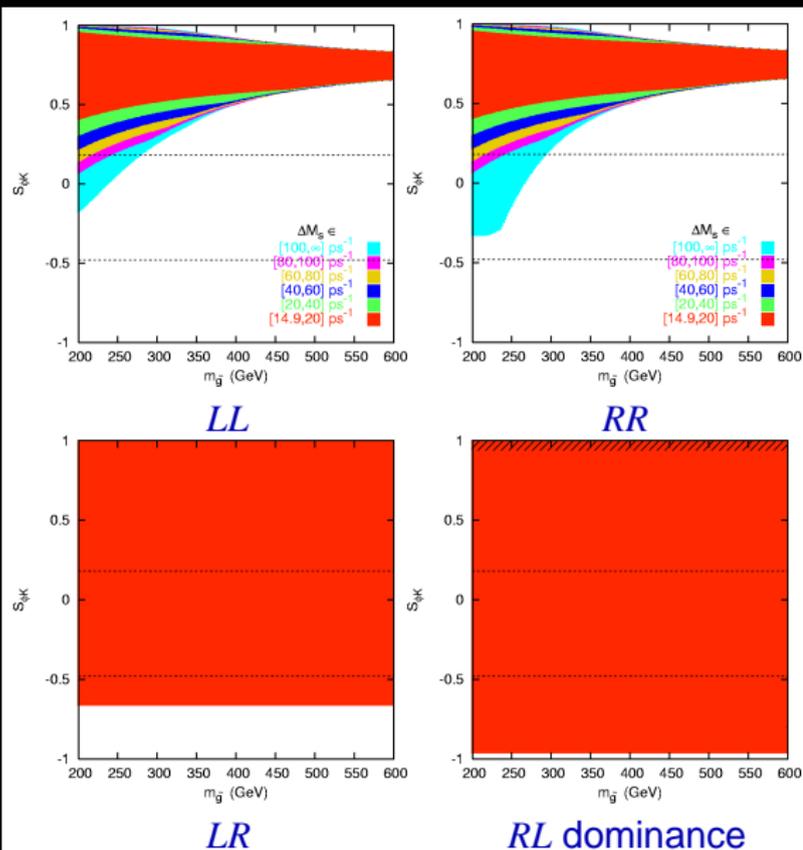


# Sparticle mass dependence

- Allow  $|\delta_{23}^d| < 1$  consistent with  $B(B \rightarrow X_s \gamma)$ .

Fix  $\frac{m_{\tilde{g}}^2}{\tilde{m}^2} = 1$ .

- For  $LL$  or  $RR$ , SUSY effect rapidly decouples as  $\tilde{m}$  increases.
- For  $LR$  or  $RL$ , SUSY effect remains constant.



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# RR insertion is well motivated

- Sizeable  $\tilde{s}_R - \tilde{b}_R$  mixing is expected in SUSY SU(5) with right-handed neutrinos.

Moroi, PLB(2000)

- Also in SUSY SO(10).

Chang, Masiero, Murayama, PRD(2003)

- U(1) flavor symmetry + SUSY may lead to large  $\tilde{s}_R - \tilde{b}_R$  mixing.

Chua, Hou, PRL(2001)

Chua, Hou, Nagashima, PRL(2004)

# $RR + RL$ double insertion greatly affects $S_{\phi K}$

Harnik, Larson, Murayama, PRD(2004)

- For large  $\tan\beta$ , an induced  $RL$  insertion can give significant (chromo)magnetic contributions.

Gabbiani, Masiero, NPB(1989)

With Baek, Jang, Ko, PRD(2000)

- This mechanism was used to explain  $S_{\phi K}^{\text{exp}} < S_{\phi K}^{\text{SM}}$ .

Diagram illustrating the mechanism of induced  $RL$  insertion. The diagram shows a loop with a gluon ( $\tilde{g}$ ) and a squark ( $\tilde{b}$ ). The external lines are  $b_L$  and  $s_R$ . The internal lines are  $\tilde{b}_L$ ,  $\tilde{b}_R$ , and  $\tilde{s}_R$ . The vertices are labeled with chromo-magnetic operators  $(\delta_{33}^d)_{RL}$  and  $(\delta_{23}^d)_{RR}$ . The diagram is proportional to  $(\delta_{23}^d)_{RR}(\delta_{33}^d)_{RL} \times \frac{m_{\tilde{g}}}{m_b}$ .

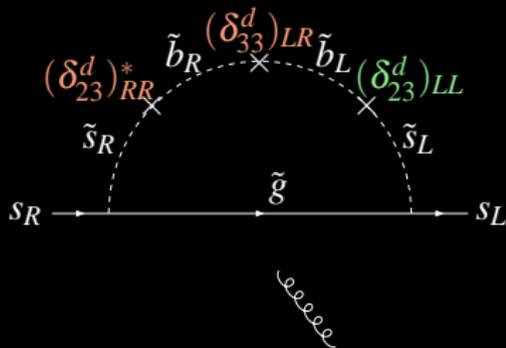
$$\propto (\delta_{23}^d)_{RR}(\delta_{33}^d)_{RL} \times \frac{m_{\tilde{g}}}{m_b}$$

$$(\delta_{33}^d)_{RL} \equiv \frac{m_b(A_b - \mu^* \tan\beta)}{\tilde{m}^2}$$

# Strange quark chromoEDM

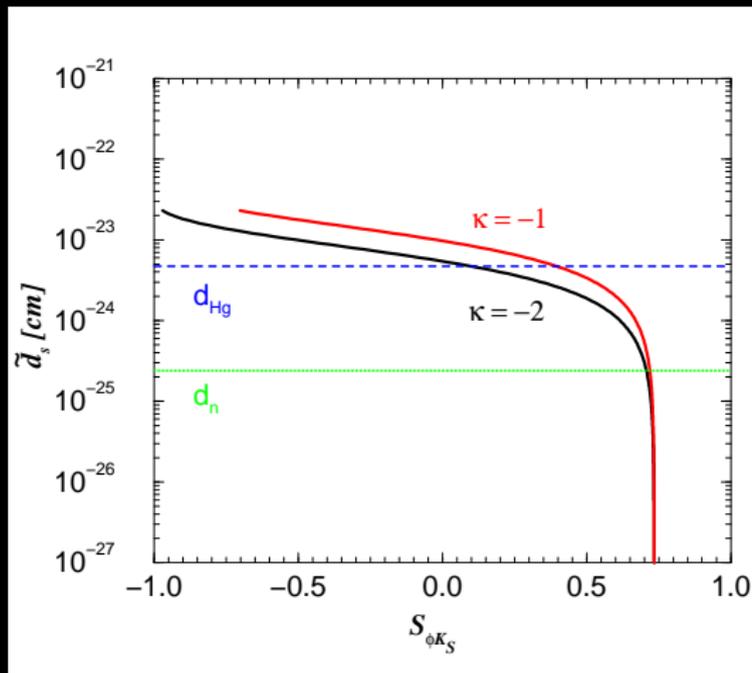
Hisano, Shimizu, PLB(2004)

- $LL$  insertions are generically expected, e.g., from RG running.
- $(\delta_{23}^d)_{LL}$  can complete a diagram for strange quark chromoEDM.



# Hadronic EDM constraints

- Correlation between strange quark CEDM  $\tilde{d}_s$  and  $S_{\phi K}$  for  $(\delta_{23}^d)_{LL} = -0.04$ .
- Lines are the upper bound on  $\tilde{d}_s$  from  $^{199}\text{Hg}$  and neutron EDM.
- $\kappa$  parameterizes uncertainty in  $\tilde{O}_{8g}$  matrix element.
- $S_{\phi K}$  strongly restricted around the SM value.



Hisano, Shimizu, PRD70(2004)

$B_d \rightarrow \eta' K_S$  CP asymmetry

- Parity transformation results in

$$\left. \frac{A^{\text{SUSY}}}{A^{\text{SM}}} \right|_{\phi K_S} \simeq (0.23 + 0.04i)[(\delta_{23}^d)_{LL} + (\delta_{23}^d)_{RR}] + (95 + 14i)[(\delta_{23}^d)_{LR} + (\delta_{23}^d)_{RL}]$$

$$\left. \frac{A^{\text{SUSY}}}{A^{\text{SM}}} \right|_{\eta' K_S} \simeq (0.23 + 0.04i)[(\delta_{23}^d)_{LL} - (\delta_{23}^d)_{RR}] + (99 + 15i)[(\delta_{23}^d)_{LR} - (\delta_{23}^d)_{RL}]$$

- Contours of  $S_{\phi K}$  and  $S_{\eta' K}$  on  $(\text{Im}(\delta_{23}^d)_{LL}, \text{Im}(\delta_{23}^d)_{RR})$  plane for  $\tilde{m} = m_{\tilde{g}} = 500$  GeV,  $\mu \tan \beta = 5$  TeV.

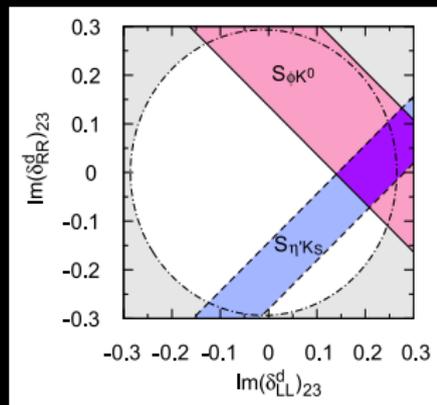
Data favors  $LL$  insertion.

Endo, Mishima, Yamaguchi, PLB(2005)  $\longrightarrow$

- But, right-handed new physics remains strangely beautiful.

Larson, Murayama, Perez, JHEP(2005)

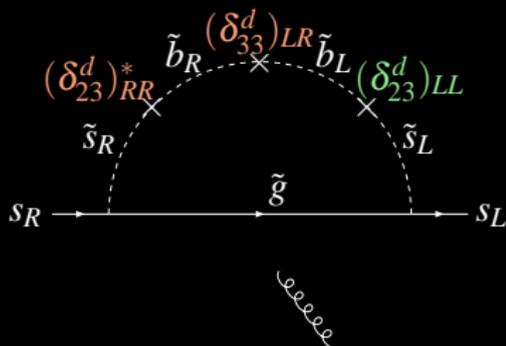
Kagan, Talk at BCP2  
Khalil, Kou, PRL(2003)



$S_{\phi K}$  and  $\varepsilon'/\varepsilon_K$ 

With P. Ko, A. Masiero, PRD(2005)

- Generically we expect  $(\delta_{13}^d)_{LL} \sim \lambda^3 \sim 8 \times 10^{-3}$ .
- $(\delta_{13}^d)_{LL}$  constitutes a diagram for  $\varepsilon'/\varepsilon_K$  in  $K_L \rightarrow \pi\pi$ .

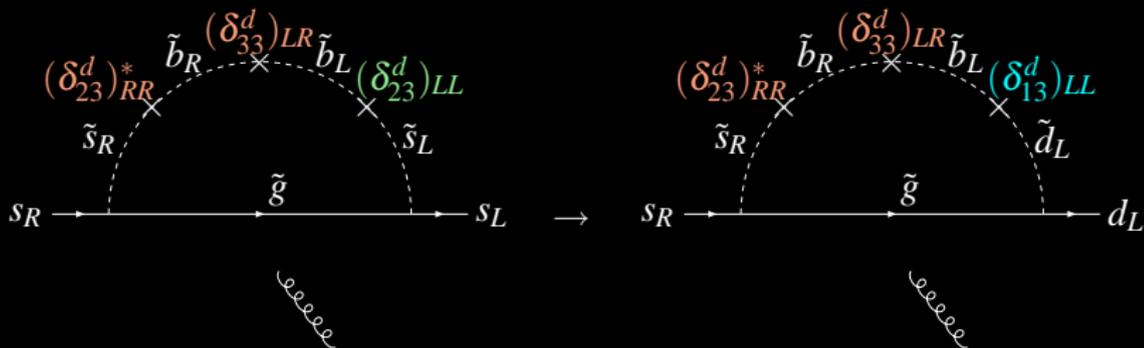


- Well known that  $(\delta_{12}^d)_{LR} \sim 10^{-5}$  can saturate  $\varepsilon'/\varepsilon_K$ .  
Gabbiani, Gabrielli, Masiero, Silvestrini, NPB(1996)
- We needed  $(\delta_{23}^d)_{RR}(\delta_{33}^d)_{RL} \sim 10^{-2}$  to significantly change  $S_{\phi K}$ .  
With Kane, Ko, Kolda, Wang $\times 2$ , PRD(2004)
- Large effect on  $\varepsilon'/\varepsilon_K$  expected from  $(\delta_{13}^d)_{LL}(\delta_{33}^d)_{LR}(\delta_{32}^d)_{RR} \sim 8 \times 10^{-5}$ .

$S_{\phi K}$  and  $\varepsilon'/\varepsilon_K$ 

With P. Ko, A. Masiero, PRD(2005)

- Generically we expect  $(\delta_{13}^d)_{LL} \sim \lambda^3 \sim 8 \times 10^{-3}$ .
- $(\delta_{13}^d)_{LL}$  constitutes a diagram for  $\varepsilon'/\varepsilon_K$  in  $K_L \rightarrow \pi\pi$ .

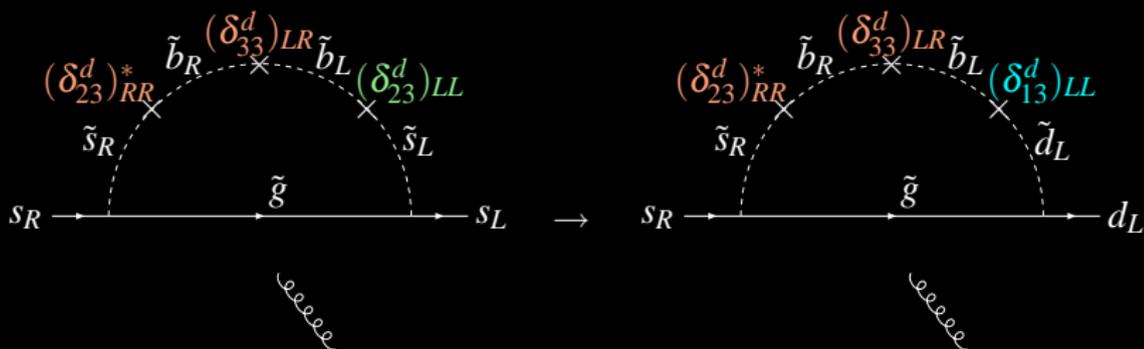


- Well known that  $(\delta_{12}^d)_{LR} \sim 10^{-5}$  can saturate  $\varepsilon'/\varepsilon_K$ .  
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# Numerical analysis

- $\Delta S = 1$  effective Hamiltonian

$$O_{8g} = -\frac{g_s}{8\pi^2} m_s \bar{d} \sigma_{\mu\nu} (1 + \gamma_5) G^{\mu\nu} s$$

$$C_{8g} = \frac{\pi \alpha_s}{\tilde{m}^2} \frac{m_{\tilde{g}}}{m_s} \left[ \frac{1}{6} N_1(x) + \frac{3}{2} N_2(x) \right] (\delta_{13}^d)_{LL} (\delta_{33}^d)_{LR} (\delta_{32}^d)_{RR}$$

- Fix  $(\delta_{13}^d)_{LL} = 8 \times 10^{-3} \times e^{-2.7i}$ ,  $\tilde{m} = m_{\tilde{g}} = 500$  GeV.

- Scan over

$$-1 \leq \text{Re}(\delta_{23}^d)_{RR}, \text{Im}(\delta_{23}^d)_{RR} \leq 1$$

imposing

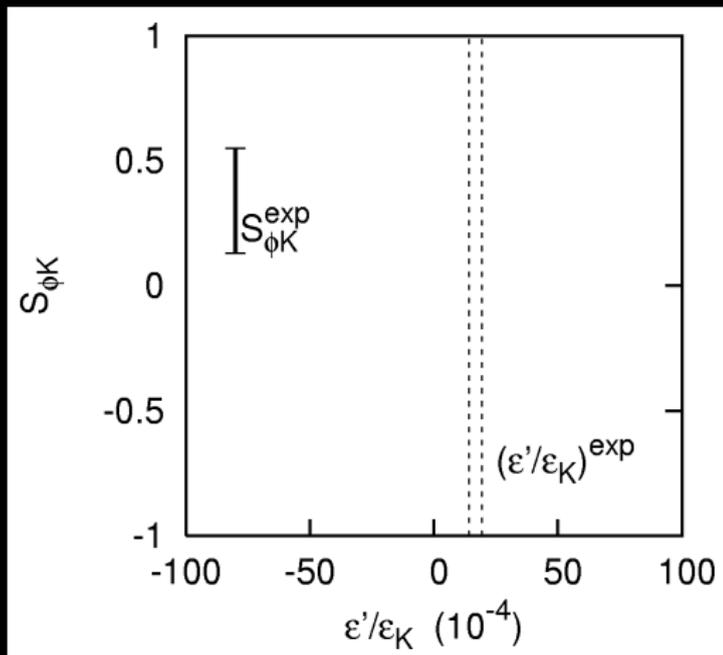
$$2.0 \times 10^{-4} \leq B(B \rightarrow X_s \gamma) \leq 4.5 \times 10^{-4},$$

$$\Delta M_s \geq 14.9 \text{ ps}^{-1}.$$

# Result for $\mu \tan \beta = 5$ TeV

- Correlation between  $S_{\phi K}$  and  $\varepsilon'/\varepsilon_K$ .
- $0.25 < S_{\phi K} < 1$   
for  
 $\varepsilon'/\varepsilon_K = (16.7 \pm 2.6) \times 10^{-4}$ .

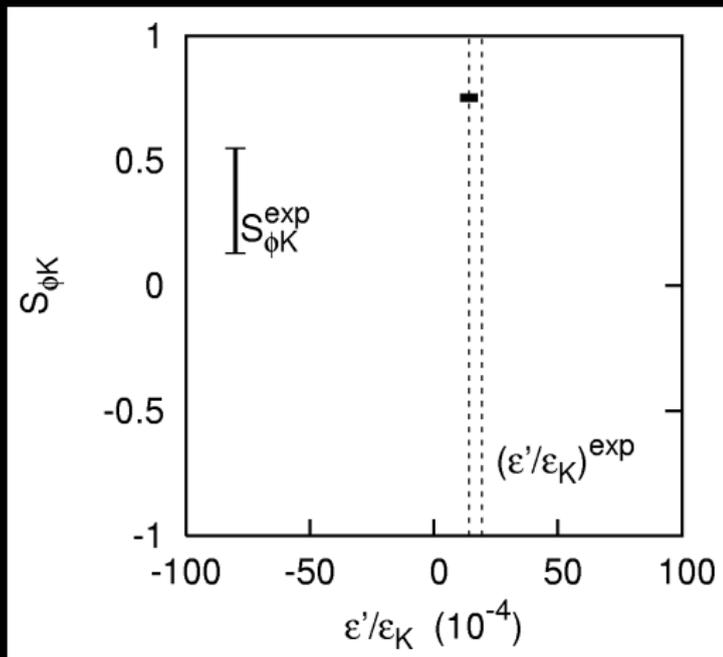
PDG 2004



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PDG 2004

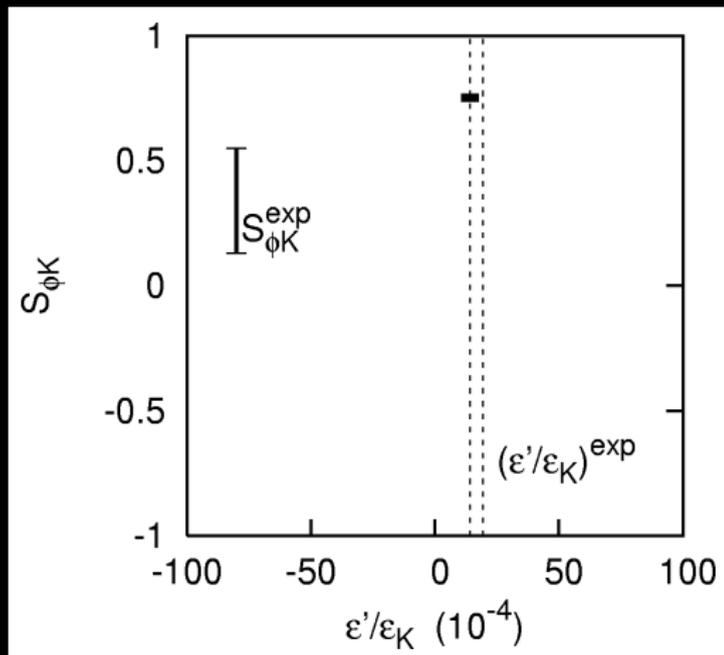
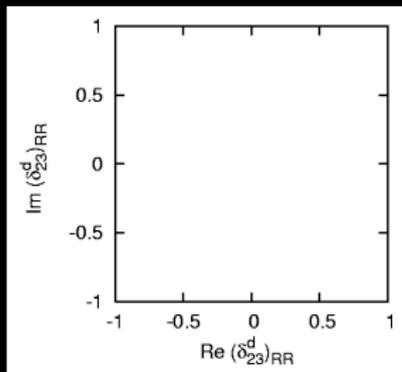


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SUSY contribution

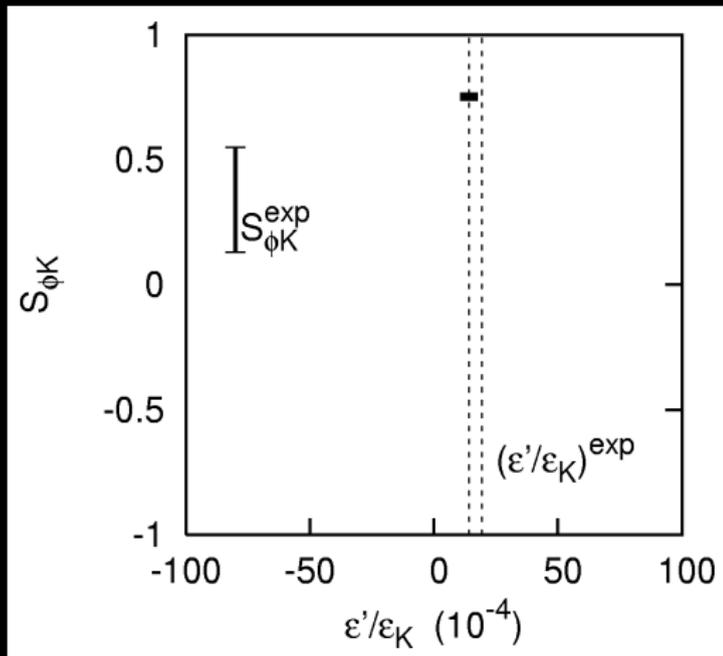
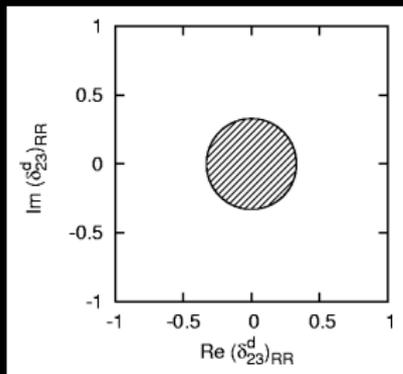


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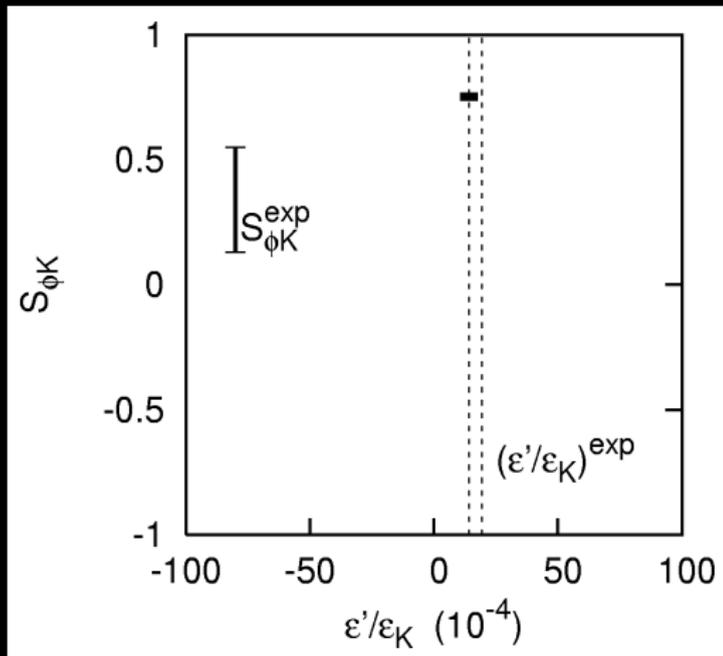
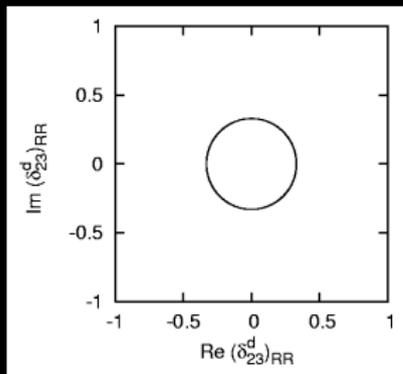
## $B(B \rightarrow X_s \gamma)$ constraint



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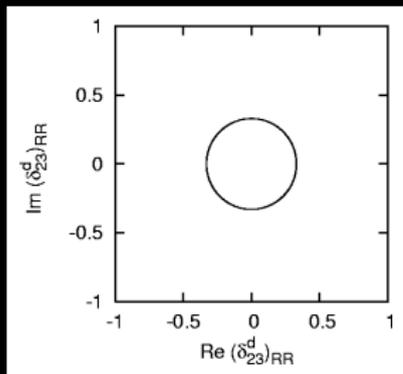
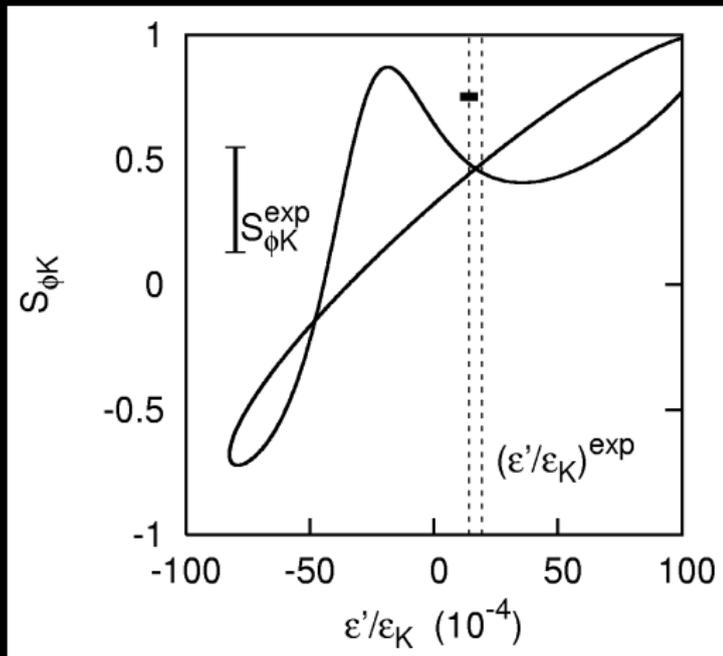
PDG 2004



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PDG 2004

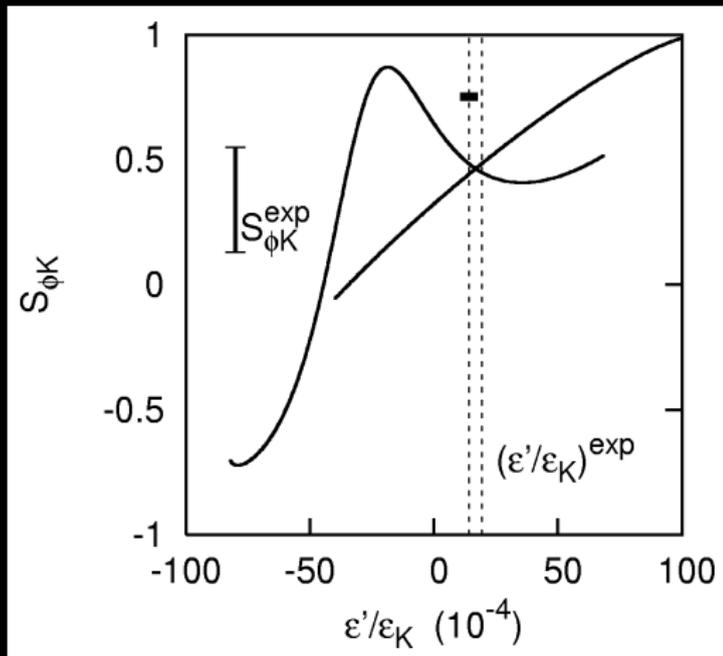
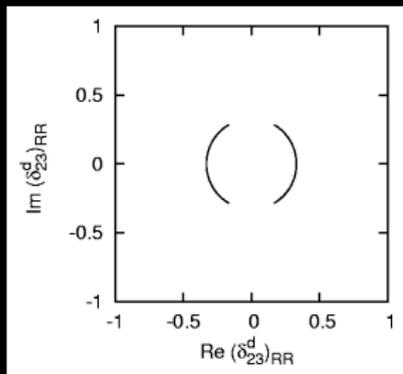


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PDG 2004

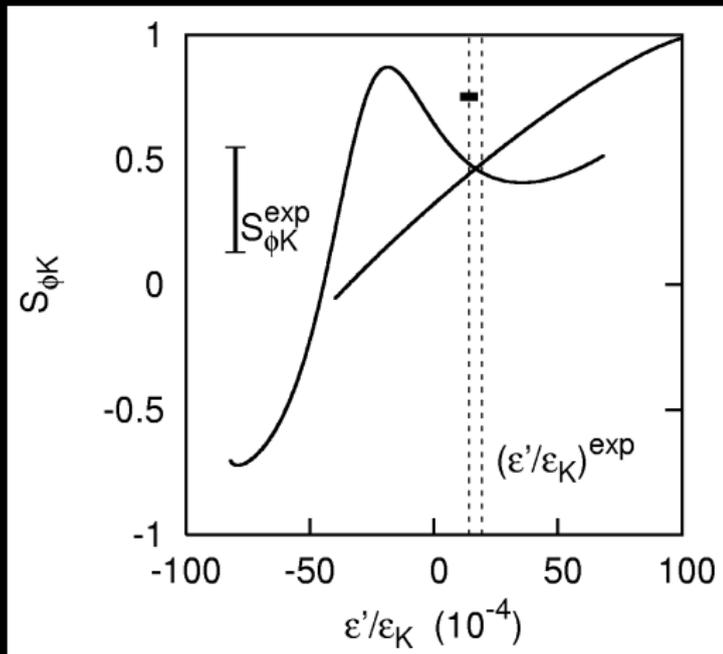
$\Delta M_s$  constraint



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PDG 2004

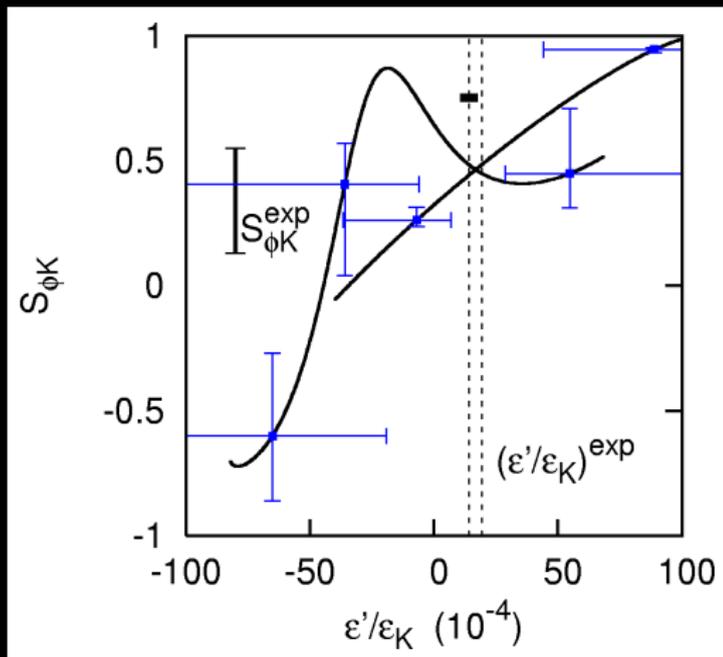


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Hadronic uncertainties

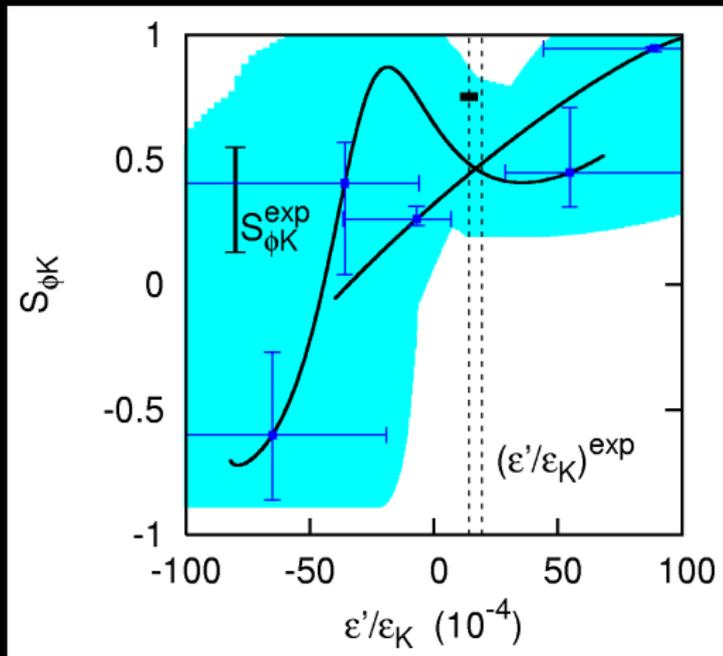


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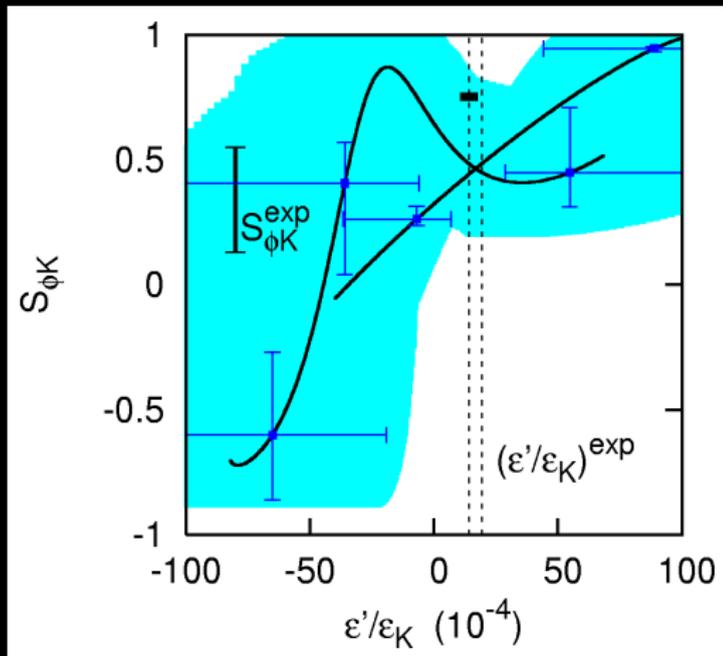


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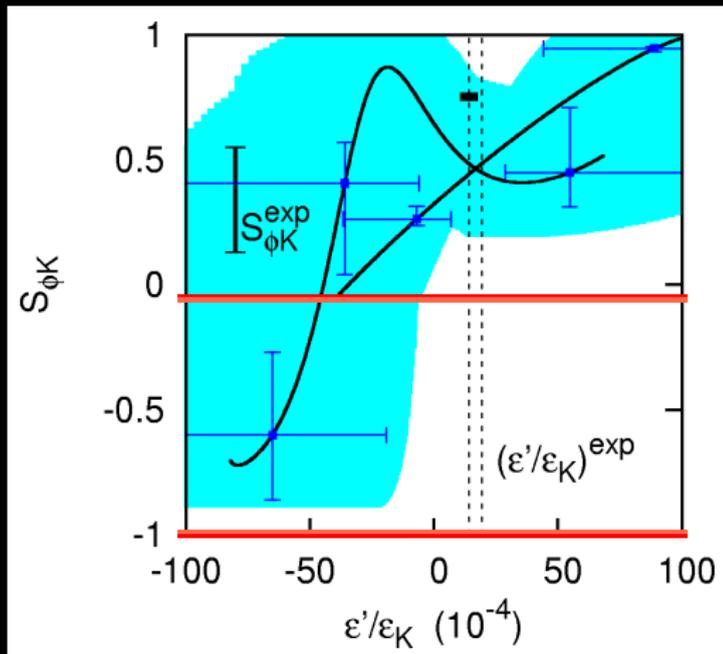
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PDG 2004

Old Belle data excludes this scenario

hep-ex/0207098



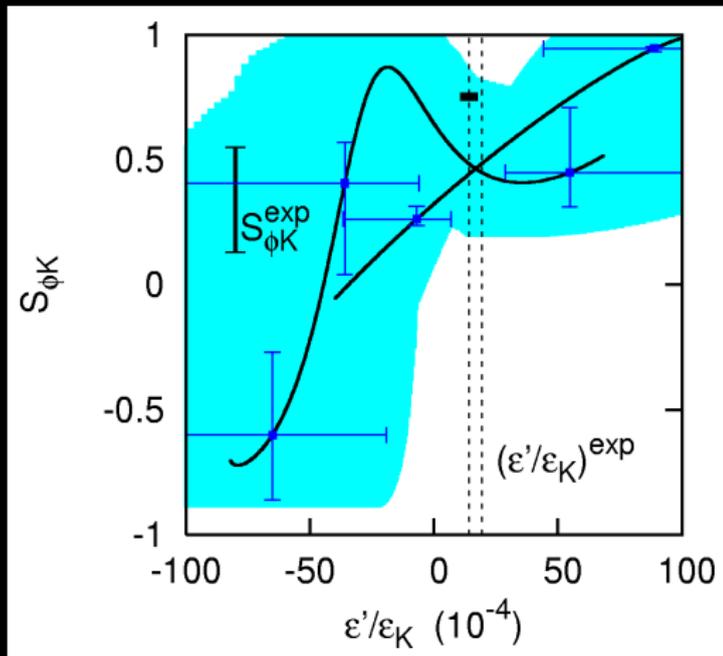
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PDG 2004

For  $S_{\eta' K}$ , do

$$(\epsilon'/\epsilon_K)_{\text{SUSY}} \rightarrow -(\epsilon'/\epsilon_K)_{\text{SUSY}}$$



# Outline

- 1  $B^0-\overline{B}^0$  mixing,  $B \rightarrow J/\psi K_S$ ,  $B \rightarrow X_d \gamma$  in general MSSM
- 2  $B_d \rightarrow \phi K_S$   $CP$  asymmetries as a probe of SUSY
- 3  $B_d \rightarrow \phi K_S$   $CP$  asymmetry and  $\varepsilon'/\varepsilon_K$
- 4 Summary

# Summary

- $B \rightarrow X_d \gamma$  strongly constrains  $(\delta_{13}^d)_{LL}$  and  $(\delta_{13}^d)_{LR}$ . Still, its direct  $CP$  asymmetry can be very different from the SM value.
- $S_{\phi K}$  is more sensitive to  $(\delta_{23}^d)_{LR}$  or  $(\delta_{23}^d)_{RL}$  than  $(\delta_{23}^d)_{LL}$  or  $(\delta_{23}^d)_{RR}$ .  $(\delta_{23}^d)_{LL}$  or  $(\delta_{23}^d)_{RR}$  can lead to large  $B_s - \bar{B}_s$  mixing.
- CPV in  $b \rightarrow s$  transitions such as  $S_{\phi K}$  can be related to  $\varepsilon' / \varepsilon_K$  in an  $RR$  mixing scenario.

# An example setup

- SU(5) GUT + right-handed neutrinos.
- Seesaw mechanism.
- Universal boundary conditions at  $M_*$ .
- Neutrino mass spectrum with normal hierarchy.
- Hierarchical neutrino Yukawa coupling eigenvalues.
  - Small  $(\delta_{12}^d)_{RR}$ ,  $(\delta_{13}^d)_{RR}$ .
  - Clear correlation between  $\varepsilon'/\varepsilon_K$  and  $S_{\phi K}$ .
- $M_N$  and  $Y_\nu$  diagonalized simultaneously.
- (Moderately) high  $\tan\beta$ .

# Radiative generation of sflavor mixing

- Left-handed squark mixings

$$\tilde{q}_j \text{---} \text{---} \text{---} \tilde{q}_i \quad \rightsquigarrow \quad (\delta_{ij}^d)_{LL} \sim V_{ii}^* V_{ij}$$

$[Y_U^\dagger Y_U]_{ij}$

$$(m_{\tilde{q}}^2)_{ij} \simeq -\frac{1}{8\pi^2} [V^\dagger \lambda_u^2 V]_{ij} (3m_0^2 + A^2) \left( 3 \log \frac{M_*}{M_{\text{GUT}}} + \log \frac{M_{\text{GUT}}}{M_W} \right)$$

- Right-handed down squark mixings

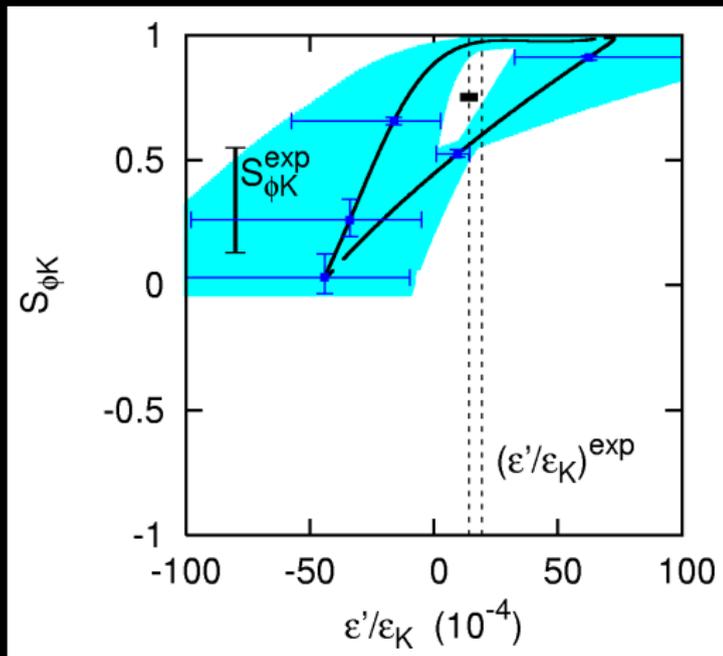
$$\tilde{d}_{Rj} \text{---} \text{---} \text{---} \tilde{d}_{Ri} \quad \rightsquigarrow \quad |(\delta_{ij}^d)_{RR}| \sim y_{V_3}^2 [V_L^*]_{3i} [V_L]_{3j}$$

$[Y_N^\dagger Y_N]_{ij}$

$$(m_{\tilde{d}}^2)_{ij} \simeq -\frac{1}{8\pi^2} e^{-i(\phi_i^{(L)} - \phi_j^{(L)})} y_{V_k}^2 [V_L^*]_{ki} [V_L]_{kj} (3m_0^2 + A^2) \log \frac{M_*}{M_{\text{GUT}}}$$

# Result for $\mu \tan \beta = 1 \text{ TeV}$

- Correlation between  $S_{\phi K}$  and  $\varepsilon'/\varepsilon_K$
  - $0.5 < S_{\phi K} < 1$  for  $\varepsilon'/\varepsilon_K = (16.7 \pm 2.6) \times 10^{-4}$ .
- PDG 2004



$\epsilon_K$ 

- Box diagrams with triple insertions of  $(\delta_{13}^d)_{LL}(\delta_{33}^d)_{LR}(\delta_{32}^d)_{RR} \equiv (\delta_{12}^d)_{LR}^{\text{eff}}$  may contribute to  $\epsilon_K$ .

- $B(B \rightarrow X_s \gamma)$  constrains

$$|(\delta_{12}^d)_{LR}^{\text{eff}}| \lesssim 2 \times 10^{-4}.$$

- $|(\epsilon'/\epsilon_K)_{\text{SUSY}}| < |(\epsilon'/\epsilon_K)_{\text{exp}}|$  implies

$$|\text{Im}(\delta_{12}^d)_{LR}^{\text{eff}}| \lesssim 2 \times 10^{-5}.$$

Gabbiani, Gabrielli, Masiero, Silvestrini, NPB(1996)

- Then,

$$\sqrt{|\text{Im}[(\delta_{12}^d)_{LR}^{\text{eff}}]^2|} \lesssim 6 \times 10^{-5},$$

- As a consequence,

$$|(\epsilon_K)_{\text{SUSY}}| \lesssim \frac{1}{30} |(\epsilon_K)_{\text{exp}}|.$$

- $\epsilon_K$  is always safe if  $\epsilon'/\epsilon_K$  constraint is satisfied.

$$\tau \rightarrow \mu \gamma$$

$$\bullet \bar{5} = \{\bar{D}, \hat{\Theta}_L^\dagger L\} \rightarrow$$

Left-handed slepton mixing is related to right-handed sdown mixing



$$\rightsquigarrow (m_{\tilde{l}}^2)_{ij} \simeq -\frac{1}{8\pi^2} y_{\nu_k}^2 [V_L]_{ki} [V_L^*]_{kj} (3m_0^2 + A^2) \log \frac{M_*}{M_{N_k}}$$

$$\sim (m_{\tilde{d}}^2)_{ij}$$

- If we impose

$$B(\tau^\pm \rightarrow \mu^\pm \gamma) < 6.8 \times 10^{-8},$$

BABAR Collaboration, hep-ex/0502032

$$|(\delta_{23}^d)_{RR}| \lesssim 0.03 \quad \text{for} \quad \tan \beta = 10 \quad \text{and} \quad Y_D = Y_E^T.$$

Ciuchini, Masiero, Silvestrini, Vempati, Vives, PRL(2004)

→ SUSY effect becomes small.

- Not much difference even if we relax  $Y_D = Y_E^T$  to account for  $m_e/m_d \neq m_\mu/m_s$ .
- Note  $(\varepsilon'/\varepsilon_K) - S_{\phi_K}$  correlation is **not specific to GUT.**