

# 超対称性とフレーバー混合

山口 昌弘(東北大)

2005年3月8日

科研費特定領域第3回研究会

「質量起源と超対称性物理の研究」

# Introduction

- 質量起源：
  - W/Z bosonの質量
  - quark/leptonの質量
    - hadronの質量は議論しない
- Electroweak Symmetry Breakdown (EWSB)
  - would-be Nambu-Goldstone bosons
  - eaten by W/Z bosons
  - W/Z massive

# Standard Model (SM)

- Two Roles of Higgs Fields:
  - Higgs: elementary scalar with  $SU(2)_L$  doublet
  - Generates masses to W/Z bosons
    - 4 degrees of freedom
    - 3 are eaten by W/Z bosons to give their masses
    - 1 remains as physical Higgs
  - target of search at collider experiments
  - Generates masses to quarks/leptons
    - Yukawa interaction
- very economical approach

# Naturalness Problem in SM

- Scalar Mass:
  - unstable against radiative corrections
  - Quadratic divergence
- Fine-tuning needed to keep EW scale small
- Probably this is a real problem.  
(cf. Cosmological Constant Problem)

# Theories/Models/Scenarios of EWSB

- Supersymmetry
- Extra-Dimensions
- Higgs as Pseudo NG boson
- Technicolor
- Composite Higgs
- Higgsless
- .....

- Dynamical EWSB
  - very attractive: Many people hate elementary scalar
  - symmetry breakdown  $\rightarrow$  NG bosons  $\rightarrow$  W/Z boson masses
  - Difficulty to generate q/l masses
    - FCNC/large top mass
- Elementary Higgs: easy to generate q/l masses  
Yukawa couplings
- SUSY: Minimal version (MSSM) is compatible with gauge coupling unification.
  - This is not the case for LED.
- SUSY: still the prime candidate for Beyond-SM (since '90)

# Supersymmetry

- A solution to naturalness problem
  - “how” problem: how is EW scale protected from huge radiative corrections?
  - “why” problem: why is EW scale so small?
- SUSY gives an answer to the “how” problem.
  - cancellation of quadratic divergence between bosons and fermions “technically natural”
- Approach to the “why” problem
  - dynamical SUSY breaking?
  - Still a big mystery (fine tuning in string landscape !?)

# SUSY phenomenology

- superparticles not far from EW scale
- light Higgs  $< \sim 130$  GeV
- gauge coupling unification
- dark matter candidate (neutralino LSP)
- possible effects in FCNC processes (B/D/K and leptons)
- possible effects in CP violation: EDMs
  
- solid framework
  - experimental study for more than 10 yrs
  - properties well-known by simulation, though not discovered yet
  - advantage to discuss FCNC as well



# Talk Plan

- Introduction
- Where is SUSY?
  - naturalness
  - dark matter argument
  - split SUSY
- SUSY around the corner !?
  - Higgs
  - g-2 of muon
  - B-physics

# *Where is SUSY?*

# Where are Superpartners?

- Lower bounds

- charginos/sleptons  $>100$  GeV (LEP)

- gluinos/squarks  $>300$  GeV (Tevatron)

- Higgs  $>114$  GeV

- stop typically heavier than 500 GeV (MSSM)

- Upper bounds on superpartners?

- difficult to answer

- Let's discuss a bit more (though no clear answer).

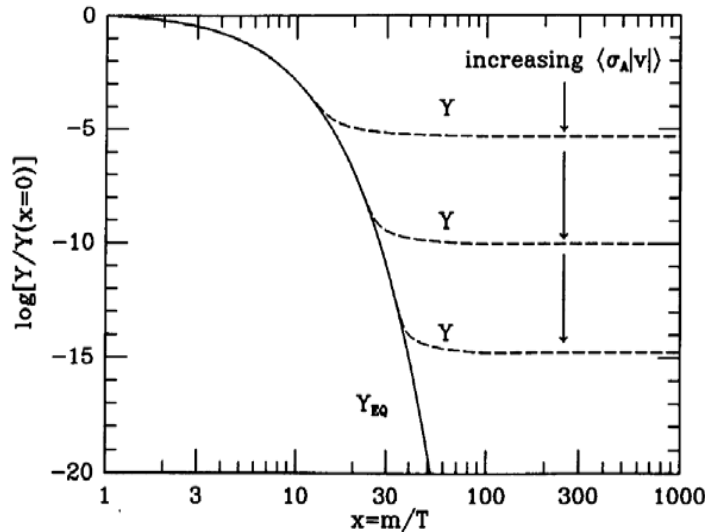
# naturalness

- naturalness/fine-tuning
  - difficult to address quantitatively
  - Usual statement: they are not far away from EW scale
  - typically(!?) within reach of LEP/ Tevatron/ LHC.... time dependent statement
- Fine-tuning may not be a criterion at all. (e.g. split SUSY) see below

# Dark Matter Argument

- SUSY provides an excellent candidate for cold dark matter: **neutralino dark matter**
- Assumptions:
  - **Neutralino LSP:**
    - A neutralino (a combination of neutral gauginos and neutral higgsinos) is lightest superparticle (LSP).
  - **R-parity conservation → LSP is stable**
  - **Thermal Relic under Standard Thermal History**
    - The Universe gradually cools down from very hot universe ( $T > 100\text{GeV}$ ) as the Universe expands. Nothing special (such as huge entropy production) happens.

# Thermal Relic Abundance

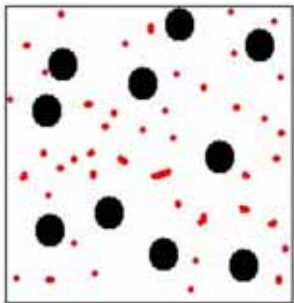


From  
Text Book by  
Kolb & Turner

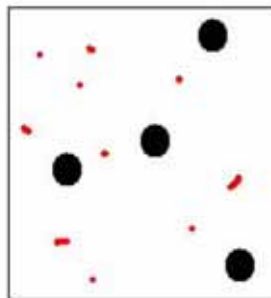
At high  $T$ , the neutralinos are in thermal equilibrium. As Universe cools down, the neutralinos get non-relativistic and their abundance is Boltzmann suppressed.

Eventually one neutralino LSP cannot find another neutralino to annihilate each other.

→ Freeze-out !



High Temp.  
2005/3/8



Low Temp.

Final Abundance is proportional to the inverse of the annihilation cross section.

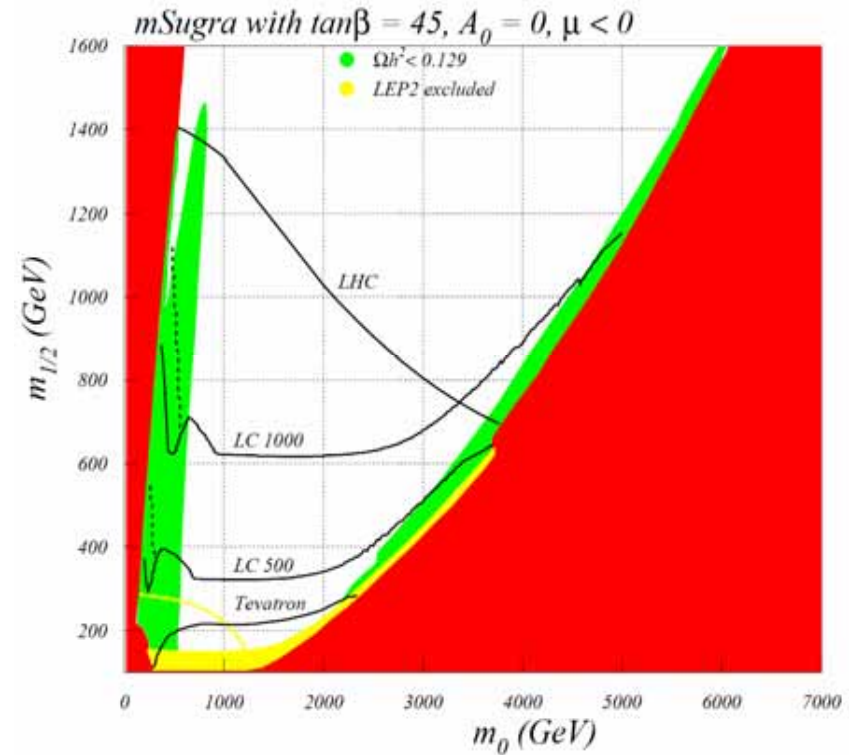
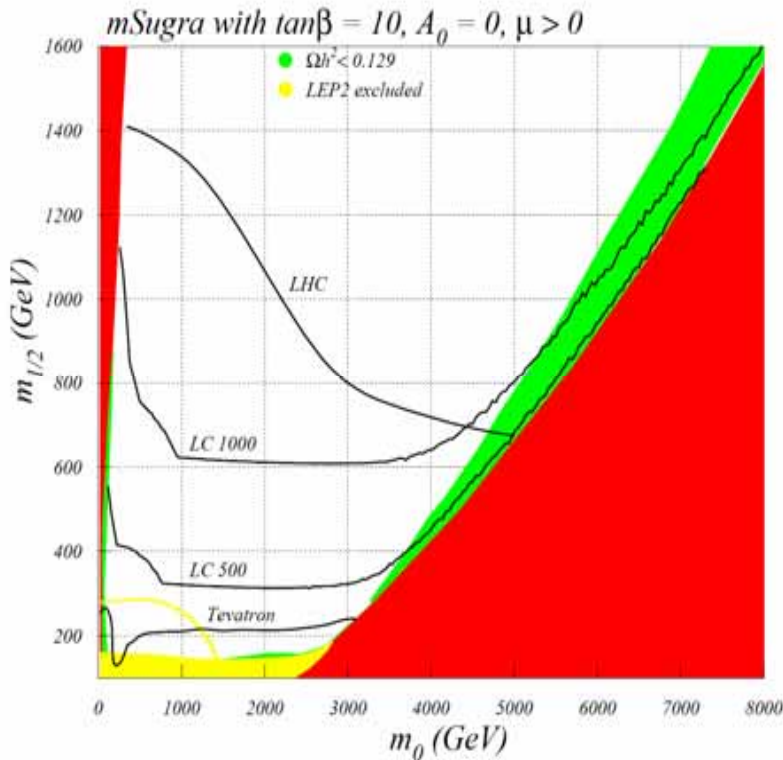
A crude estimate:

$$\Omega h^2 \sim 1 \times (\langle \sigma_{\text{ann}} v \rangle / 10^{-10} \text{ GeV}^{-2})^{-1}$$

motivation for WIMPs

# Discovery Reach at Tevatron/ LHC/ ILC

Baer, Belyaev, Krupovnickas & Tata '03



Even LHC may not be able to cover the whole region.

- No practical upper bound on superparticle masses from the dark matter argument
  - co-annihilation with stau: very effective to reduce the relic abundance
  - (Annihilation into  $W$  is also effective in higgsino LSP.)
- Remember that the argument relies on the three assumptions.



# Split Supersymmetry

Arkani-Hamed,  
Dimopoulos 04

- New scenario motivated by string landscape
  - landscape:

この世はfine tuningでできた 終末思想?

- scalar massのfine tuning は気にしない!

開き直り!?

# Split Supersymmetry (cont.)

- scalar masses  $\gg$  gaugino masses, higgsino masses
  - × naturalness
    - Higgs mass  $\sim 150\text{-}160$  GeV
    - No SUSY FCNC
    - No SUSY CP
    - dark matter
    - gauge coupling unification
  - phenomenology
    - long-lived (practically stable) gluinos
  - will be (dis)proved in future collider experiments

# ***SUSY around the corner !?***

# Some Hints on New Physics

- Higgs Mass
- $(g-2)$  of muon
- B-physics: CP asymmetry in  $B \rightarrow \phi K, \eta' K$

# Higgs Mass

(although Higgs is a part of SM)

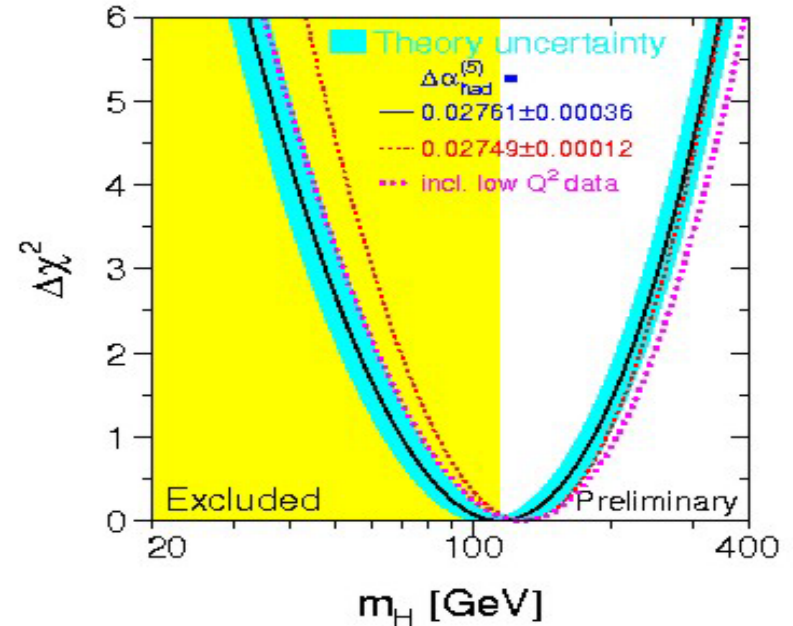
Current limit from direct search

$$m_h(\text{MSM}) > 114 \text{ GeV}$$

(Smoking Gun Events at LEP II !?)

Global fit prefers light Higgs (in minimal SM)

$$m_h(\text{MSM}) = 114^{+69}_{-45} \text{ GeV}$$



# Higgs in MSSM

$m_h < m_Z = 91$  GeV at tree-level

← quartic coupling given by gauge coupling

Top-stop loop → raises  $m_h$  significantly

Large radiation correction needed to raise  $m_h$  above 114 GeV (especially for low  $m_t$ ): Heavy SUSY mass spectrum preferred

“little hierarchy problem in SUSY”

Higgs is waiting to be discovered in MSSM.

We expect Tevatron to tell us crucial information on Higgs.

Note: Higgs mass is very sensitive to top mass

–  $m_t = 174$  GeV → 178 GeV pushes up  $m_h$  by 2 GeV or so.

# $(g - 2)_\mu$ : Current Status

Values of  $a_\mu = (g-2)_\mu / 2$

Experiment : 0.0011659203(7) ( $\mu^-$  included) PDG2004

SM prediction: 0.00116591763(74)

e.g. Hagiwara et al 2004 based on  $e^+e^- \rightarrow \pi^+\pi^-$

$$\delta a_\mu \sim 26(10) \times 10^{-10}$$

still more than 2-sigma deviation

cf. situation in year 2001:

Exp. 0.0011659202(14)(6)

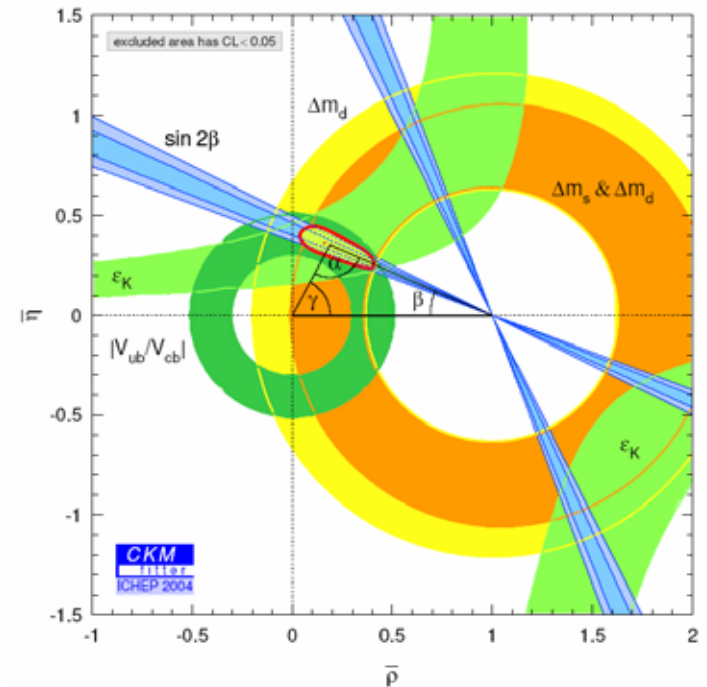
$$\delta a_\mu \sim 43(16) \times 10^{-10}$$

# B physics

- CP asymmetry in  $b \rightarrow c$  transition:
  - measurement of  $\sin 2\beta$  ( $\phi_1$ )
  - good agreement with SM.

The Kobayashi-Maskawa framework has been established.

- $b \rightarrow s$  penguin is now a hot subject.





# $B \rightarrow S$ penguin is interesting

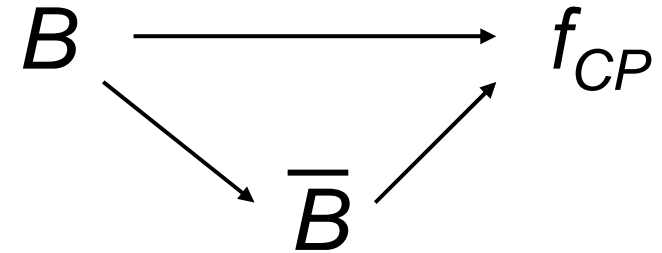
- $b \rightarrow c$  tree level in SM
- $b \rightarrow s$  loop level in SM
  - Increasing chance to see **New Physics Effects**
  - Not fully explored yet
- Prejudice: **Mixing between 2-3 generation may be large**, as suggested by atmospheric neutrino.

# Time dependent CP asymmetry of $B \rightarrow \phi K$ & $B \rightarrow \eta' K$

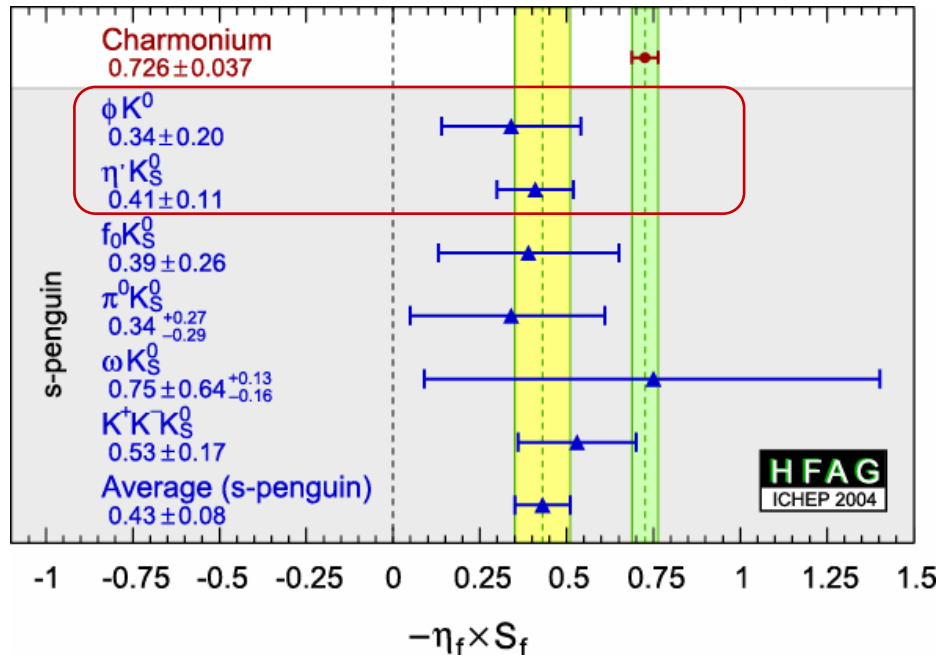
- mixing-induced CP asymmetry

$$a_{CP}(t) \equiv \frac{\Gamma(\bar{B}(t) \rightarrow f_{CP}) - \Gamma(B(t) \rightarrow f_{CP})}{\Gamma(\bar{B}(t) \rightarrow f_{CP}) + \Gamma(B(t) \rightarrow f_{CP})}$$

$$= \frac{|\lambda|^2 - 1}{|\lambda|^2 + 1} \cos \Delta mt + \frac{2\text{Im}\lambda}{|\lambda|^2 + 1} \sin \Delta mt$$



- B-factoriesの実験の現状 (summer 2004)



$S_{\phi K^0}$

Belle  $0.06 \pm 0.33 \pm 0.09$

BaBar  $0.50 \pm 0.25^{+0.07}_{-0.04}$

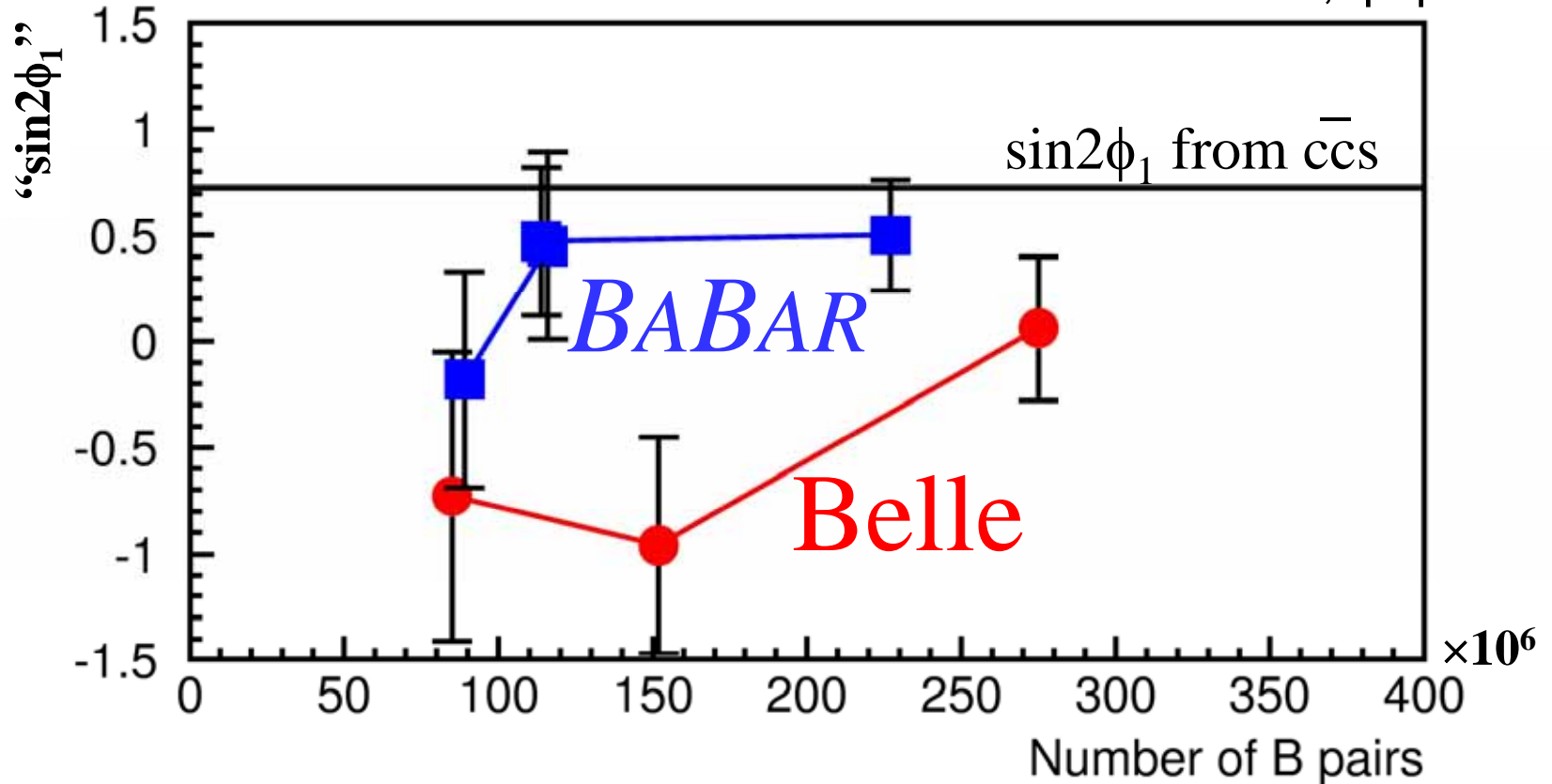
$S_{\eta' K_S}$

Belle  $0.65 \pm 0.18 \pm 0.04$

BaBar  $0.27 \pm 0.14 \pm 0.03$

# History of “ $\sin 2\phi_1$ ” with $\phi K^0$

Hazumi, fpcp2004



- Clearly we need more data of year 2005, 2006, 2007,... to say something definite.
- Stay tuned!
  
- A new feature:
  - Apparent anomalies are seen in more than one mode!  
( $B \rightarrow \phi K$  and  $B \rightarrow \eta' K$ )

-- Ken-Ichi Hikasa  
talk in the same meeting  
last year

# How theorists behave

---

- Wait and see
  - 99% of 99%CL “new physics” will go away
- Play and enjoy
  - Write as much papers as you can, before it goes away
  - If real, you may hit a gold mine

Take the second approach! In fact we wrote a paper and are preparing another one.

Let us consider SUSY interpretation.

# FCNC and CP in SUSY SM

New sources of flavor mixing (with CP violation):

soft SUSY breaking terms

- eg. squark masses, slepton masses (3x3 matrices, non-diagonal)

SM: FCNC is suppressed by GIM mechanism

SUSY contribution: No GIM suppression for arbitrary choice of soft masses

→ Too large FCNC for weak scale SUSY

“SUSY FCNC problem”

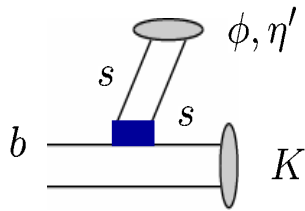
Sensible Choice of soft masses required:

Various proposals:

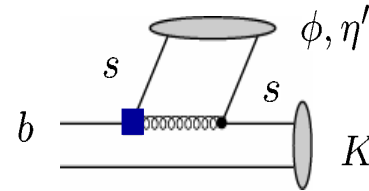
- Universal sfermion masses: mSUGRA, gauge mediation,...
- Aligned sfermion masses: flavor symmetry,.....

# SUSY contribution to $B \rightarrow \phi K, \eta' K$

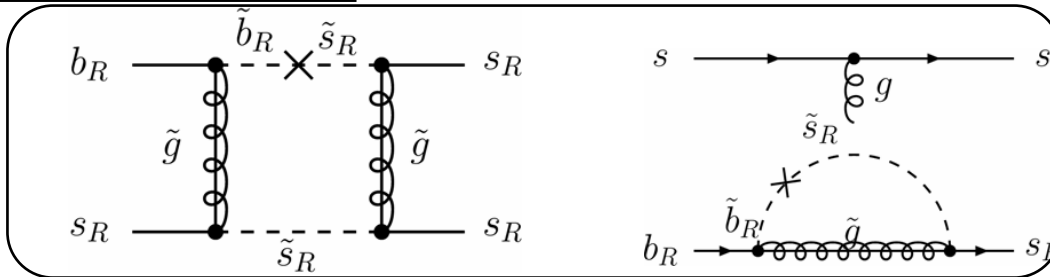
four-quark



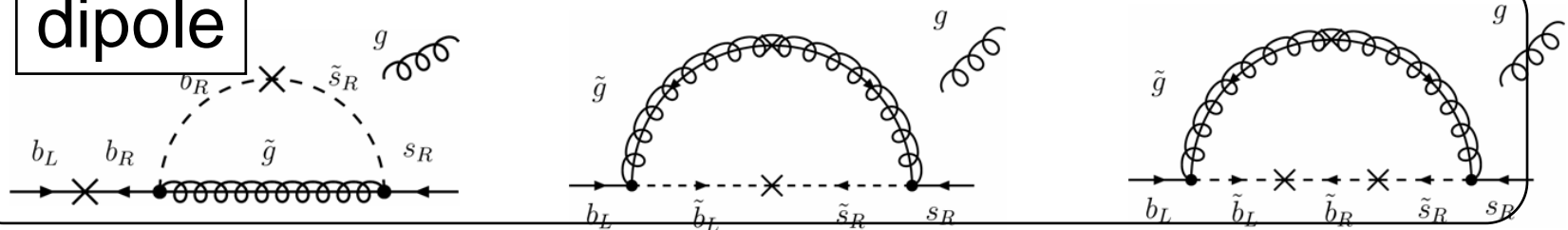
chromo-dipole



four-quark



dipole



# Left-Handed (LH) vs Right-Handed (RH)

- SM:  $W$ -loop,  $V$ - $A$  current (LH structure)
- NP: Both chiralities can arise.
  - Pattern of NP contribution depends on chirality structure of flavor violation in NP
- SUSY: Flavor mixing in squark masses
  - LH (SU(2) doublet) squarks
  - RH (SU(2) singlet) squarks



# RH vs LH in “SDOWN” sector

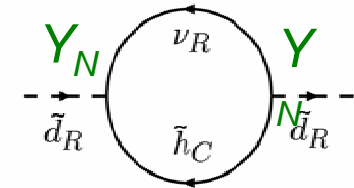
- RH:

- Large 2-3 RH sdown mixing in SUSY GUT see-saw models

(Moroi 01)

- Atmospheric neutrino implies large 2-3 mixing in neutrino Yukawa
- SUSY GUTs → large 2-3 mixing in RH sdown sector
- Large contribution to  $B \rightarrow \phi K$

- Cf. solar neutrino → Kaon physics



- LH:

- Renormalization Group Flow: does not give significant flavor mixing with new CP phase

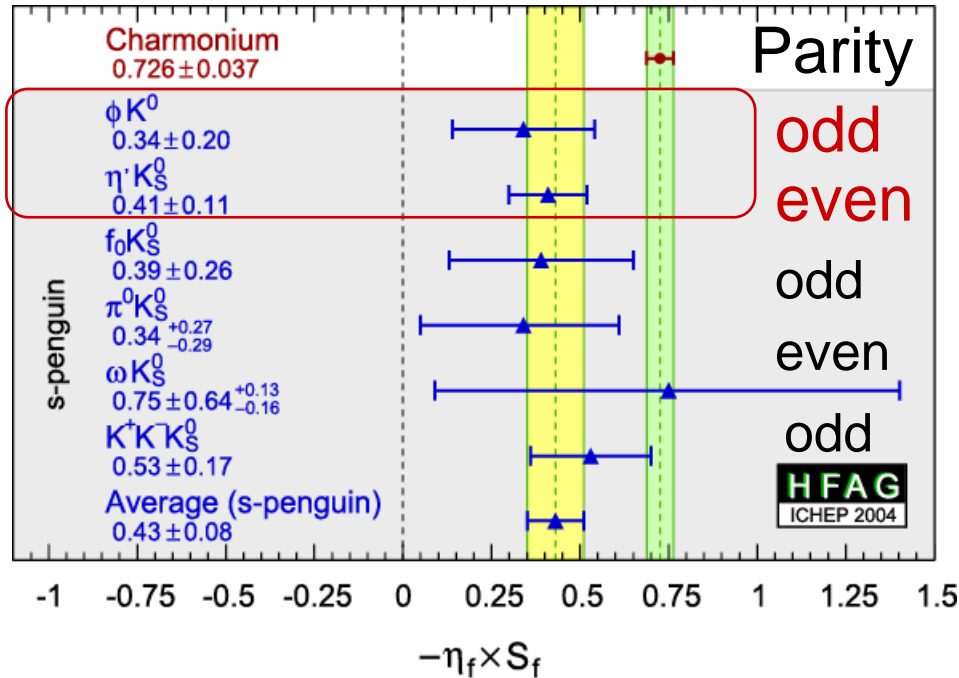
- May be imprinted at Ultra-High Energy Scale

- Flavor symmetry!?

- Large 2-3 neutrino mixing may also give large 2-3 mixing in LH squark sector.

# A SUSY Interpretation of Current Data

Endo, Mishima & MY hep-ph/0409245

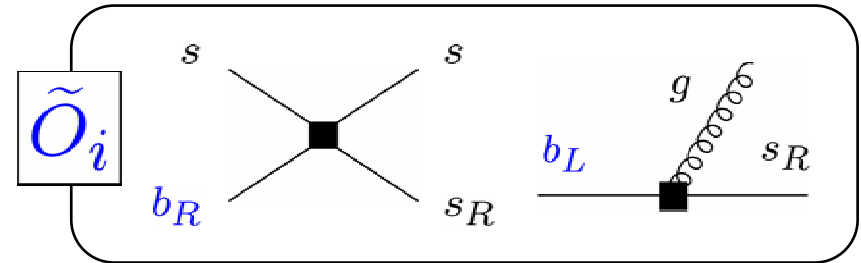
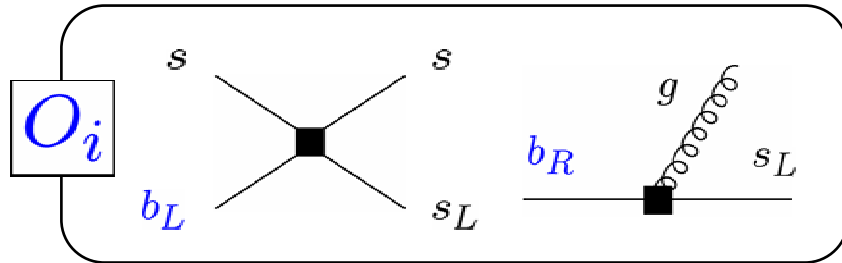


Key Points:

1. Anomalies in more than one mode  
( $\phi K, \eta' K$ )
2. The final states have opposite parity.

# Sign of Contributions by Final-state Parity

- Effective Hamiltonian  $H_{\text{eff}} \sim C_i O_i + (\tilde{C}, \tilde{O} : R \leftrightarrow L)$



- Decay Amplitude  $\langle f | \tilde{O}_i | B_d \rangle = -(-1)^{P_f} \langle f | O_i | B_d \rangle$

$$A \sim [C_i - (-1)^{P_f} \tilde{C}_i] \langle f | O_i | B_d \rangle$$

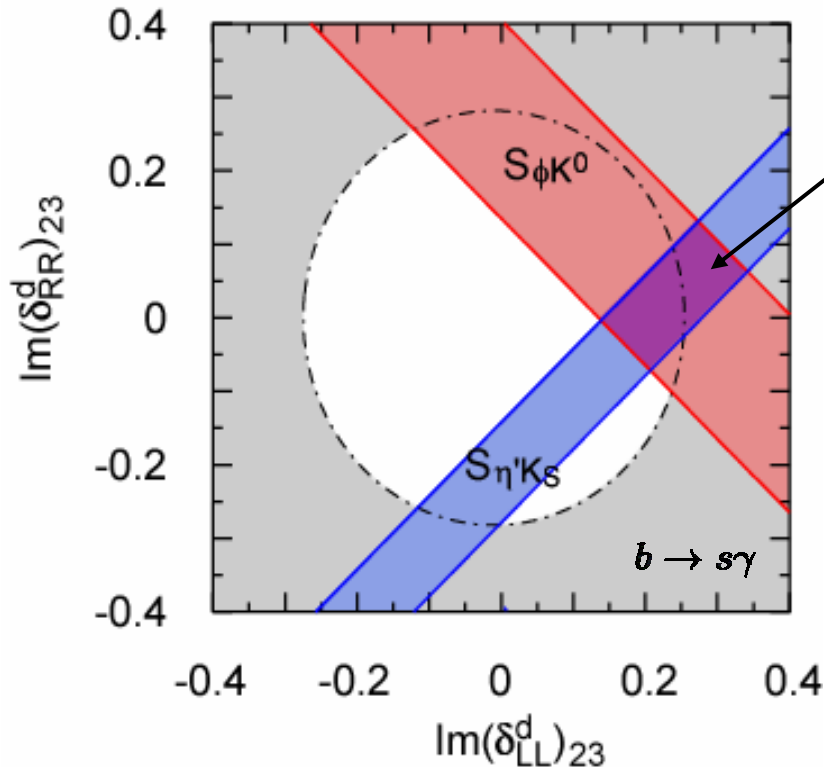
Kagan; Khalil&Kou

$$A_i^{\text{NP}}(\phi K) \propto [C_i^{\text{SM}} + C_i^{\text{NP}} + \tilde{C}_i^{\text{NP}}] \langle \phi K | O_i | B_d \rangle$$

$$A_i^{\text{NP}}(\eta' K) \propto [C_i^{\text{SM}} + C_i^{\text{NP}} - \tilde{C}_i^{\text{NP}}] \langle \eta' K | O_i | B_d \rangle$$

# Numerical Estimation of $S_{b-s}$ in MSSM

Endo, Mishima & MY 04



favored by current data  
from B-factories ( $1\sigma$ )

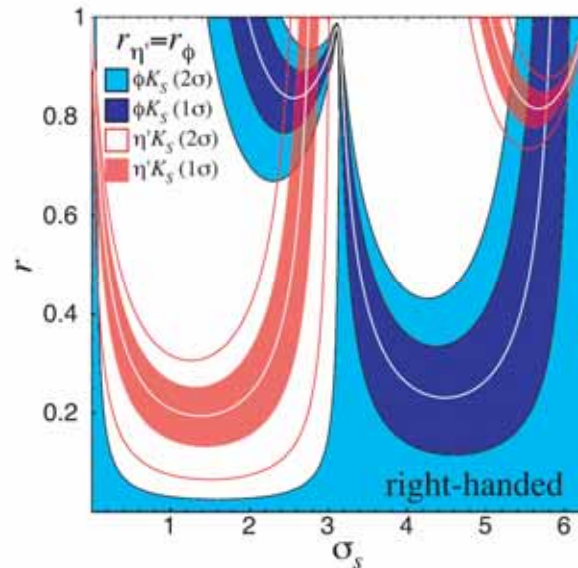
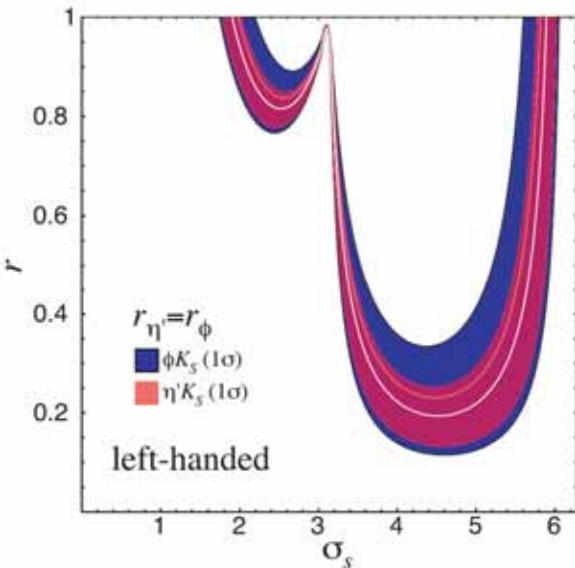
*The current data  
prefers LH dominant  
case!*

$$(\delta_{LL,RR}^d)_{23} = (m_{\tilde{d}_{L,R}}^2)_{23}/m_{\tilde{q}}^2$$

$$m_{\text{soft}} = 500 \text{ GeV}, \tan \beta = 10$$

$$\text{GF: } q^2 = m_b^2/2$$

# RH completely excluded?



Larson,  
Murayama  
& Perez 04

$$\mathcal{A}(B^0 \rightarrow \phi, \eta') = \mathcal{A}_{\phi, \eta'}^{\text{SM}} (1 \pm r_{\phi, \eta'} e^{i\sigma_s})$$

LH interpretation:

OK for generic  
choice of CP phase

RH interpretation:

may marginally work for  
special choice of CP  
phase and  $r \sim 1$   
(danger of  $b \rightarrow s$  gamma etc)

← detailed study  
(Endo, Mishima & MY, in  
preparation)

# Lesson from this analysis

Future confirmation of the s-penguin anomalies will tell us

- not only the existence of NP
- but also **the pattern of chiral structure (and hopefully more structure) of the NP.**



**Determination of Wilson coefficients**

**Usage of more than one mode is crucial!**

# Prospects

More Data on s-penguin: wait and watch!

Correlation with other B decay processes

e.g.  $B_s - \bar{B}_s$  mixing:  $\Delta m_s \geq 20 - 100 \text{ ps}^{-1}$

$Br(B \rightarrow \mu^+ \mu^-)$  can be  $10^{-7} \gg 10^{-9}$  (SM)

Correlation with Lepton Flavor Violation

$\tau \rightarrow \mu\gamma, \tau \rightarrow \mu\eta$  etc

$\mu \rightarrow e\gamma$  etc

# Conclusions

- SUSY: 腐ってもSUSY
  - the prime candidate for Beyond-SM
- Sparticles/Higgs Searches → Lower bounds
- No Clear Upper bounds on Sparticle Masses
- EW precision data prefers light Higgs
  - top発見の直前の状況に似ている
  - Expect Evidence (?) from Tevatron RUN II
- Some anomalies:
  - g-2 of muon
  - CP in  $b \rightarrow s$  penguin **More data from B-factories to conclude**
- We also expect
  - discovery of superparticles
  - dark matter detection
  - new events such as LFV  $B_s - \bar{B}_s$   $B \rightarrow \mu^+ \mu^-$